

## Hint for 7b in Assignment 6

Given a graph  $G = (V, E)$ , where  $V$  is the set of the vertices and  $E$  is the set of edges, construct a graph  $H$  in the following way. Set  $n = |V|$ .

- Subdivide every edge of  $G$  into two edges by adding a new vertex in the middle of that edge.
- Add a separate clique of size  $100n^2$  to the graph. That is, add a set of  $100n^2$  new pairwise adjacent vertices  $u_1, \dots, u_{100n^2}$ .
- Join  $u_1$  to every vertex in  $V$ .

What is the relation between the size of the “maximum clique in  $G$ ” and the size of the “maximum 2-clique in  $H$ ”?