- 1. (10 points) Problem 6.2.
- 2. (10 points) Problem 6.5.
- 3. (10 points) Problem 6.6.
- 4. (10 points) Problem 11.3. (Hint: Follow the argument for the 2-approximation algorithm for the survivable network design problem and instead of a  $\frac{1}{2}$ -edge argue that there is a 1-edge. Use a different token argument where 1 token for an edge is given  $\frac{x_{uv}}{2}$  for vertex constraints of u and v and rest  $1 x_{uv}$  to the smallest set in laminar family containing both u and v. Then show that the above token argument does give one token to each constraint and achieve a contradiction.)
- 5. (10 points) In an instance of the minimum bounded weighted-degree spanning tree we are given a graph G = (V, E) and cost function  $c : E \to \mathbb{R}^+$ , a weight function  $w : E \to \mathbb{R}^+$ , a degree bound  $B_v$  on each vertex v, and the task is to find a spanning tree T with minimum cost and  $\sum_{e \in \delta_T(v)} w(e) \leq B_v$  for all  $v \in V$ . Give a good bi-criteria approximation algorithm for the problem.