

# Compositional Semantics: Quantification and Underspecification

COMP-599

Oct 31, 2016

# Announcements

## Final presentation slot

E-mail me by next Monday if your slot doesn't work for you.

## Proposal

If your proposal has a green circle on it, it means I'm worried about some aspect of it. You can come talk to me and/or submit a second proposal if you'd like.

## **Make-up pre-midterm office hours:**

Tuesday, Nov 8, from 2:30pm – 4pm

# Midterm

Wednesday, Nov 9, in class, 80 min.

Closed book

Question types:

- M/C
- Short answer
- Problem solving

# Expectations

You'll be expected to know:

- Definitions (including formulas)
- How to run algorithms by hand
- Simple derivations
- Simple probability and calculus (up to, say, chain rule)
- Basic linguistic terminology and theory
- Lambda calculus

You won't be expected to remember\*:

- Lagrange multipliers
- What the derivative of, say,  $e^x$  is.
- Specific lexical rules for translating items into FOL

\*But could still be asked to apply or use, given relevant facts

# How To Study

Review and redo the exercises we did in class

Learn the definitions of all the technical terms (most of them are in bold or are the titles of slides)

Review your assignments

Do practice problems

Do the practice midterm

List of practice problems from the textbook are on the course website. Note that they are not meant to be comprehensive, but are supplementary.

# Outline

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Syntax-driven semantic composition

Quantifiers

Generalized quantifiers

Underspecification

# Syntax-Driven Semantic Composition

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Augment CFG trees with lambda expressions

- Syntactic composition = function application

Semantic attachments:

$A \rightarrow \alpha_1 \dots \alpha_n$        $\{f(\alpha_j.sem, \dots, \alpha_k.sem)\}$

syntactic composition

semantic attachment

# Proper Nouns

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Proper nouns are FOL constants

$$PN \rightarrow COMP599 \quad \{COMP599\}$$

Actually, we will **type-raise** proper nouns

$$PN \rightarrow COMP599 \quad \{\lambda x. x(COMP599)\}$$

- It is now a function rather than an argument.
- We will see why we do this.

NP rule:

$$NP \rightarrow PN \quad \{PN.sem\}$$



# Common Nouns

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Common nouns are predicates inside a lambda expression of type  $\langle e, t \rangle$

- Takes an entity, tells you whether the entity is a member of that class

$N \rightarrow student \quad \{\lambda x. Student(x)\}$

Let's talk more about common nouns next class when we also talk about quantifiers.

# Intransitive Verbs

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We introduce an *event variable*  $e$ , and assert that there exists a certain event associated with this verb, with arguments.

$$V \rightarrow rules \quad \{\lambda x. \exists e. Rules(e) \wedge Ruler(e, x)\}$$

Then, composition is

$$S \rightarrow NP VP \quad \{NP.sem(VP.sem)\}$$

Let's derive the representation of the sentence "*COMP-599 rules*"

# Neo-Davidsonian Event Semantics

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Notice that we have changed how we represent events

**Method 1:** multi-place predicate

*Rules(x)*

**Method 2:** Neo-Davidsonian version with event variable

$\exists e. Rules(e) \wedge Ruler(e, x)$

Reifying the event variable makes things more flexible

- Optional elements such as location and time, passives
- Add information to the event variable about tense, modality

# Transitive Verbs

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Transitive verbs

$V \rightarrow enjoys$

$\{\lambda w. \lambda z. w(\lambda x. \exists e. Enjoys(e) \wedge Enjoyer(e, z) \wedge Enjoyee(e, x))\}$

$VP \rightarrow V NP$

$\{V.sem(NP.sem)\}$

$S \rightarrow NP VP$

$\{NP.sem(VP.sem)\}$

**Exercise:** verify that this works with the sentence “*Jackie enjoys COMP-599*”

# Quantifiers

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## Universal quantifiers

- *all, every*

*All students like COMP-599.*

$\forall x. \text{Student}(x) \rightarrow \text{Like}(x, \text{COMP-599})$

## Existential quantifiers

- *a, an, some*

*Some/A student likes COMP-599.*

$\exists x. \text{Student}(x) \wedge \text{Like}(x, \text{COMP-599})$

Why  $\rightarrow$  for the universal quantifier, but  $\wedge$  for the existential one?

# Russell (1905)'s Definite Descriptions

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How to express “*the student*” in FOL?

e.g., *The student took COMP-599.*

Need to enforce three properties:

1. There is an entity who is the student.
2. There is at most one thing being referred to who is a student.
3. The student participates in some predicate, here, “*took COMP-599*”.

# The King of France is Bald

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Property 1 is important. Consider “*The King of France is bald.*”

## Solution 1:

- Define a new constant for KING-OF-FRANCE, much like for proper nouns.

FOL MR becomes *Bald*(KING–OF–FRANCE)

What is the problem with this solution?

# Definite Articles

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*The student took COMP-599:*

1. There is an entity who is the student.
2. There is at most one thing being referred to who is a student.
3. The student participates in some predicate.

What is the range of this existential quantifier?

$$\exists x. Student(x) \wedge \forall y. (Student(y) \rightarrow y = x) \\ \wedge took(x, COMP-599)$$

For simplicity, for now, assume took is a predicate, rather than use event variables.



# Incorporating into Syntax

Now, let's incorporate this to see how lambda calculus can deal with this compositionally.

Semantic attachment for lexical rule for *every*:

$Det \rightarrow every \quad \{\lambda P. \lambda Q. \forall x. P(x) \rightarrow Q(x)\}$

What do  $P$  and  $Q$  represent?

# Every Student Likes COMP-599

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$Det \rightarrow every \quad \{\lambda P. \lambda Q. \forall x. P(x) \rightarrow Q(x)\}$

$NP \rightarrow Det N \quad \{Det.sem(N.sem)\}$

Let's do the derivation of *Every student likes COMP-599*.

Recall:

$VP \rightarrow V NP \quad \{V.sem(NP.sem)\}$

$S \rightarrow NP VP \quad \{NP.sem(VP.sem)\}$

$V \rightarrow likes$

$\{\lambda w. \lambda z. w(\lambda x. \exists e. Likes(e) \wedge Liker(e, z) \wedge Likee(e, x))\}$

Using explicit event variables again.

# Questions and Exercise

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What are the lexical rules with semantic attachments for *a*? For *the*?

Come up with the derivation of *COMP-599 likes every student*.

# Adjectives

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Can we figure out the pattern for adjectives?

*student*

$\lambda x. Student(x)$

*smart student*

$\lambda x. Smart(x) \wedge Student(x)$

*smart*

?

Also need an augmented rule for  $N \rightarrow A N$

# Scopal Ambiguity: Multiple Quantifiers

What are the possible readings for the following?

*Every student took a course.*

This is known as **scopal ambiguity**.

# Scopal Ambiguity

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*Every student took a course.*

*every* > *a*

$\forall x. \text{Student}(x)$

$\rightarrow (\exists y. \text{Course}(y) \wedge \exists e. \text{took}(e) \wedge \text{taker}(e, x) \wedge \text{takee}(e, y))$

*a* > *every*

$\exists y. \text{Course}(y)$

$\wedge (\forall x. \text{Student}(x) \rightarrow \exists e. \text{took}(e) \wedge \text{taker}(e, x) \wedge \text{takee}(e, y))$

Would like a way to derive **both** of these readings from the syntax. What would we get with our current method?

# Underspecification

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**Solution:** Derive a representation that allows for both readings

**Underspecified representation** – A meaning representation that can embody all *possible* readings without explicitly enumerating all of them.

Other cases where this is useful:

- We are genuinely missing some information (e.g., the tense information), so we choose not to include it in the meaning representation.

# Cooper Storage (1983)

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Associate a **store** with each FOL expression that allows both readings to be recovered.

*Every student took a course.*

$\exists e. \text{took}(e) \wedge \text{taker}(e, s_1) \wedge \text{takee}(e, s_2)$

$(\lambda Q. \forall x. \text{Student}(x) \rightarrow Q(x), 1),$

$(\lambda Q. \exists y. \text{Course}(y) \wedge Q(y), 2)$



# Recovering the Reading

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Once we know which reading we want (e.g., by looking at the context), recover the store:

1. Select order to incorporate quantifiers
2. For each quantifier:
  - Introduce lambda abstraction over the appropriate index variable
  - Do beta-reduction

# Example: 1, then 2

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*Every student took a course.*

$$\begin{aligned} & \exists e. \text{took}(e) \wedge \text{taker}(e, s_1) \wedge \text{takee}(e, s_2) \\ & (\lambda Q. \forall x. \text{Student}(x) \rightarrow Q(x), 1), \\ & (\lambda Q. \exists y. \text{Course}(y) \wedge Q(y), 2) \end{aligned}$$

1 first:

$$\begin{aligned} & (\lambda Q. \forall x. \text{Student}(x) \rightarrow Q(x)) \\ & (\lambda s_1. \exists e. \text{took}(e) \wedge \text{taker}(e, s_1) \wedge \text{takee}(e, s_2)) \\ & = \forall x. \text{Student}(x) \rightarrow \exists e. \text{took}(e) \wedge \text{taker}(e, x) \wedge \text{takee}(e, s_2) \end{aligned}$$

Then 2:

$$\begin{aligned} & (\lambda Q. \exists y. \text{Course}(y) \wedge Q(y)) \\ & (\lambda s_2. \forall x. \text{Student}(x) \rightarrow \exists e. \text{took}(e) \wedge \text{taker}(e, x) \wedge \text{takee}(e, s_2)) \\ & = \exists y. \text{Course}(y) \wedge \forall x. \text{Student}(x) \rightarrow \exists e. \text{took}(e) \wedge \text{taker}(e, x) \wedge \\ & \text{takee}(e, y) \end{aligned}$$

# Compositional Rules

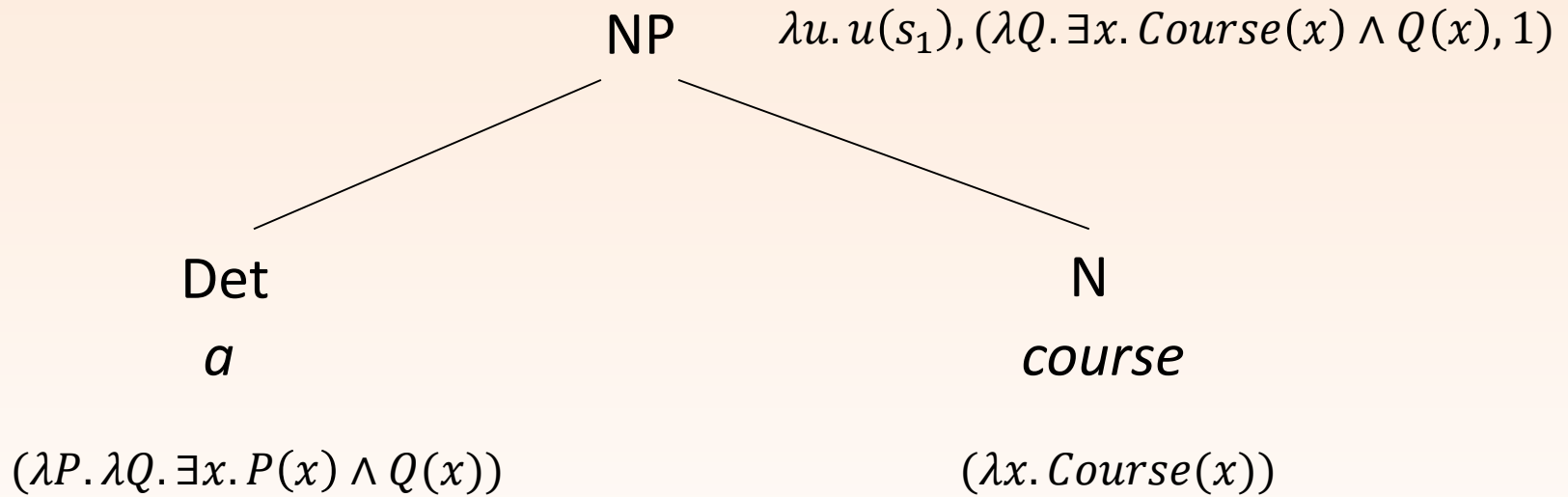
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We also need new rules with semantic attachments for our quantifiers:

- Composing quantifier with N is now modifying the *inside* part of a store
- An NP is now introduces a new index variable, which is wrapped in a lambda expression

# A Course

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What is the semantic attachment for NP  $\rightarrow$  Det N? Use .sem.store to access the store.

# Exercise

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Finish the derivation for the underspecified representation of *Every student took a course*.

Recall:

$VP \rightarrow V NP$                      $\{V.sem(NP.sem)\}$

$S \rightarrow NP VP$                      $\{NP.sem(VP.sem)\}$

$V \rightarrow took$

$\{\lambda w. \lambda z. w(\lambda x. \exists e. Took(e) \wedge Taker(e, z) \wedge Takee(e, x))\}$

$Det \rightarrow every$                      $\{(\lambda P. \lambda Q. \forall x. P(x) \rightarrow Q(x))\}$

$N \rightarrow student$                      $\{\lambda x. Student(x)\}$

# Question

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How would we disambiguate between the possible readings?

# Machine Learning Approaches

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- Higgins and Sadock, 2003. A Machine Learning Approach to Modeling Scope Preferences. *Computational Linguistics*.
- Mehdi Manshadi and James Allen. 2011. Unrestricted Quantifier Scope Disambiguation. *TextGraphs-6 Workshop*.

Frame as a classification task. Higgins and Sadock investigate for two quantifiers, Manshadi and Allen extend it to  $> 2$  quantifiers.

# Higgins and Sadock

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Class labels:

- 0        No scopal interaction
- 1        First quantifier > second quantifier
- 2        Second quantifier > first quantifier

Features

- POS tags
- Quantifiers themselves as lexical items
- Positions of the two relative to each other in the syntax tree, and the intervening nodes

Tried several standard classifiers (Naïve Bayes, MaxEnt (a.k.a. logistic regression), perceptron)



# Results

**Table 7**

Performance of the single-layer perceptron, summed over all 10 test runs.

Condition	Correct	Incorrect	Percentage correct
First has wide scope	182	99	$182/281 = 64.8\%$
Second has wide scope	35	29	$35/64 = 54.7\%$
No scope interaction	468	77	$468/545 = 85.9\%$
Total	685	205	$685/890 = 77.0\%$

Why is 77.0% perhaps a bit misleading?

# Other Aspects of Semantics

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Plurals; count vs. mass nouns

Tense, aspect, time

Modality

- Epistemic modality (how likely is something?)

- Deontic modality (you *should* or *must* do something)

Semantics beyond the sentence level

- Reference resolution (e.g., pronouns, anaphora)

There are formal analyses for all of these, and statistical models for most of them too (but some more than others).