

**RHYTHMS ANALYSIS: STEINER TREES AND DIRECTED SWAP
DISTANCE - Nov. 3, 2006**

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Contents

A Centers of the 2 Families of <i>Binary</i> Rhythms	3
B Centers of the Corresponding 2 Families of <i>Ternary</i> Rhythms	9

Appendix A

Centers of the 2 Families of *Binary Rhythms*

Dataset 4:

```
[xx.xx.x.]      'ArgentinianMilonga'  
[xx.xx.x.]      'AfroVenezuelanDrums'  
[x..xx.x.]      'Habanera'  
[xx.xx.x.]      'DetailedFromZambaFoot'  
[x.xx...x.]     'DocmioVar1c1'  
[xx.x...x.]     'DocmioVar1c2'  
[..xx...x.]      'DocmioVar1d1'  
[.x.x...x.]     'DocmioVar1d2'  
[x.xx...xx]      'DocmioVar2c'  
[xx.x...xxx]     'DocmioVar4c'  
[xx.x....x]     'DocmioVar6c'  
[x..x....]       'DocmioVar5a'  
[x..xxxx.]       'DocmioVar4a'
```

Dataset 5:

```
[xx.xx.x.x...x..x.]  'BinarizedZambaFootPlusMolossus'  
[x..x...x...x.x...]  'Binarized6_8ClaveSon'  
[x..x...x...x.x.x.]  'Binarized6_8ClaveSonVar1'  
[x..x...x...x.x.x.]  'Binarized6_8ClaveSonVar2'  
[x..x...xx...x.x...x]  'BinarizedBembe'  
[x..x...x...x...x...]  'RareBinarizedClaveSon'
```

Dataset 4 - Hamming MinSum Set

The minsum point(s) are:

[xx.x..x.] DocmioVar1c2

The minsum distance is: 23

Dataset 4 - Hamming MinMax Set

The minmax point(s) are:

[xx.x..x.] DocmioVar1c2

The minmax distance is: 3

Dataset 4 - Hamming MinSum

The minsum point(s) are:

[xx.x..x.] DocmioVar1c2

The minsum distance is: 23

Dataset 4 - Hamming MinMax

The minmax point(s) are:

[x..x..x.] Rhythm not found in database...

[x..x..xx] Rhythm not found in database...

[xx.x..x.] DocmioVar1c2

The minmax distance is: 3

Dataset 4 - Directed Swap MinSum Set

The minsum point(s) are:

[xx.x..x.] DocmioVar1c2

The minsum distance is: 24

Dataset 4 - Directed Swap MinMax Set

The minmax point(s) are:

[x..xx.x.] Habanera

[x.xx..x.] DocmioVar1c1

[xx.x..x.] DocmioVar1c2

[.x.x..x.] DocmioVar1d2

The minmax distance is: 4

Dataset 4 - Directed Swap MinSum

The minsum point(s) are:

[x..x..x.] Rhythm not found in database...

[xx.x..x.] DocmioVar1c2

The minsum distance is: 24

Dataset 4 - Directed Swap MinMax

The minmax point(s) are:

[x..x..x.] Rhythm not found in database...

The minmax distance is: 3

Dataset 5 - Hamming MinSum Set

```
-----  
The minsum point(s) are:  
[x..x..x...x.x...] Binarized6_8ClaveSon  
[x..x..x...x.x.x] Binarized6_8ClaveSonVar1  
[x..x..x...x.x.x] Binarized6_8ClaveSonVar1  
The minsum distance is: 13
```

Dataset 5 - Hamming MinMax Set

```
-----
```

```
The minmax point(s) are:  
[x..x..x...x.x.x] Binarized6_8ClaveSonVar1  
[x..x..x...x.x.x] Binarized6_8ClaveSonVar1  
The minmax distance is: 6
```

Dataset 5 - Hamming MinSum

```
-----
```

```
The minsum point(s) are:  
[x..x..x...x.x...] Binarized6_8ClaveSon  
[x..x..x...x.x.x] Binarized6_8ClaveSonVar1  
The minsum distance is: 13
```

Dataset 5 - Hamming MinMax

```
-----
```

```
The minmax point(s) are:  
[x..x..x.....] Rhythm not found in database...  
[x..x..x.....x.] Rhythm not found in database...  
[x..x..x.....xx] Rhythm not found in database...  
[x..x..x.....x.x.] Rhythm not found in database...  
[x..x..x.....x....] Rhythm not found in database...  
[x..x..x.....x...x] Rhythm not found in database...  
[x..x..x.....x...xx] Rhythm not found in database...  
[x..x..x.....xx...x] Rhythm not found in database...  
[x..x..x.....xx...xx] Rhythm not found in database...  
[x..x..x.....xx...xx] Rhythm not found in database...  
[x..x..x....x...x.] Gahu  
[x..x..x....xx....] Soukous  
[x..x..x....xx...x.] Rhythm not found in database...  
[x..x..x....xxx.x.] Rhythm not found in database...  
[x..x..x.x.....] Rhythm not found in database...  
[x..x..x.x.....x] Rhythm not found in database...  
[x..x..x.x.....xx] Rhythm not found in database...  
[x..x..x.x....x...x] Rhythm not found in database...  
[x..x..x.x....x...xx] Rhythm not found in database...  
[x..x..x.x....xx...x] Rhythm not found in database...  
[x..x..x.x....xx...xx] Rhythm not found in database...  
[x..x..x.x....xx...xx] Rhythm not found in database...  
[x..x..x.x....x....x] Rhythm not found in database...  
[x..x..x.x....x...xx] Rhythm not found in database...  
[x..x..x.x....xx...x] Rhythm not found in database...  
[x..x..x.x....xx...xx] Rhythm not found in database...  
[x..x..x.x....xx...xx] Rhythm not found in database...  
[x..x..x.x....x....x] Rhythm not found in database...
```



```
[xx.x..x....xx..x] Rhythm not found in database...
[xx.x..x....xx.xx] Rhythm not found in database...
[xx.x..x....x.....] Rhythm not found in database...
[xx.x..x....x...x.] Rhythm not found in database...
[xx.x..x....x.x.x.] Rhythm not found in database...
[xx.x..x....xx....] Rhythm not found in database...
[xx.x..x....xxx...] Rhythm not found in database...
[xx.x..x....xxx.x.] Rhythm not found in database...
[xx.x..x.x....x...] Rhythm not found in database...
[xx.x..x.x....x..x] Rhythm not found in database...
[xx.x..x.x....x.xx] Rhythm not found in database...
[xx.x..x.x.x.....] Rhythm not found in database...
[xx.x..x.x.x.x....] Rhythm not found in database...
[xx.x..x.x.x.x.x.] Rhythm not found in database...
[xx.x..x.x.xxx....] Rhythm not found in database...
[xx.x..xx.....] Rhythm not found in database...
[xx.x..xx.....x..] Rhythm not found in database...
[xx.x..xx.....x.x] Rhythm not found in database...
[xx.x..xx....xx...] Rhythm not found in database...
[xx.x..xx....xx.x.] Rhythm not found in database...
[xx.x..xxx....x...] Rhythm not found in database...
[xx.x..xxx....x.x.] Rhythm not found in database...
[xx.xx.x....x...x] Rhythm not found in database...
[xx.xx.x....x.xx] Rhythm not found in database...
[xx.xx.x....x.....] Rhythm not found in database...
[xx.xx.x....x.x..] Rhythm not found in database...
[xx.xx.x....x.x.x.] Rhythm not found in database...
[xx.xx.x....xxx....] Rhythm not found in database...
[xx.xx.x....x.x.x.] Rhythm not found in database...
[xx.xx.xx....x....] Rhythm not found in database...
[xx.xx.xx....x.x..] Rhythm not found in database...
```

The minmax distance is: 5

Dataset 5 - Directed Swap MinSum Set

The minsum point(s) are:

```
[x..x..x....x.x.x.] Binarized6_8ClaveSonVar1
[x..x..x....x.x.x.] Binarized6_8ClaveSonVar1
```

The minsum distance is: 12

Dataset 5 - Directed Swap MinMax Set

The minmax point(s) are:

```
[x..x..x....x.x.x.] Binarized6_8ClaveSonVar1
[x..x..x....x.x.x.] Binarized6_8ClaveSonVar1
```

The minmax distance is: 5

Dataset 5 - Directed Swap MinSum

```
-----  
The minsum point(s) are:  
[x..x..x...x.x.x.] Binarized6_8ClaveSonVar1  
The minsum distance is: 12
```

```
Dataset 5 - Directed Swap MinMax
```

```
-----  
The minmax point(s) are:  
[.x.x..x...x.x.] Rhythm not found in database...  
[x....x.x...x.x.] Rhythm not found in database...  
[x..x...x....x.x.] Rhythm not found in database...  
[x...x..x....xx..x.] Rhythm not found in database...  
[x...x..x...x.x.x.] Rhythm not found in database...  
[x...x..x...x.x..x.] Rhythm not found in database...  
[x...x..x.x....x.x.] Rhythm not found in database...  
[x...x..x.x.x....x.] Rhythm not found in database...  
[x...x.xx...x...x.x.] Rhythm not found in database...  
[x..xx.x....x.x.x.] Rhythm not found in database...  
The minmax distance is: 4
```

Appendix B

Centers of the Corresponding 2 Families of *Ternary* Rhythms

Dataset 6:

```
[xxxx.x]      'TribrachPlusTrochee'  
[xxxxx.]     'ZambaFoot1'  
[x.xxx.]      'Choriamb'  
[xxxxx.]     'ZambaFoot2'  
[xxx.x.]      'MolossusVar1c1'  
[xxx.x.]      'MolossusVar1c2'  
[.xx.x.]      'MolossusVar1d1'  
[.xx.x.]      'MolossusVar1d2'  
[xxx.xx]      'MolossusVar2c'  
[xxxxxx]      'MolossusVar4c'  
[xxx..x]      'MolossusVar6c'  
[x.x...]      'MolossusVar5a'  
[x.xxxx]      'MolossusVar4a'
```

Dataset 7:

```
[xxxxx.x.x.x.]   'ZambaFootPlusMolossus'  
[x.x.x..x.x..]   'The6_8ClaveSon'  
[x.x.x..x.x.x]   'The6_8ClaveSonVar1'  
[x.x.x..x.xx.]   'The6_8ClaveSonVar2'  
[x.x.xx.x.x.x]   'TernaryBembe'  
[x.x.x..x.x..]   'TernaryClaveSon'
```

Dataset 6 - Hamming MinSum Set

The minsum point(s) are:

[xxx.x.] MolossusVar1c1

[xxx.x.] MolossusVar1c1

The minsum distance is: 19

Dataset 6 - Hamming MinMax Set

The minmax point(s) are:

[xxxxx.] ZambaFoot1

[xxxxx.] ZambaFoot1

[xxx.x.] MolossusVar1c1

[xxx.x.] MolossusVar1c1

[xxx.xx] MolossusVar2c

The minmax distance is: 3

Dataset 6 - Hamming MinSum

The minsum point(s) are:

[xxx.x.] MolossusVar1c1

The minsum distance is: 19

Dataset 6 - Hamming MinMax

The minmax point(s) are:

[x.x.xx] Rhythm not found in database...

[xxx.x.] MolossusVar1c1

[xxx.xx] MolossusVar2c

[xxxx..] Rhythm not found in database...

[xxxxx.] ZambaFoot1

The minmax distance is: 3

Dataset 6 - Directed Swap MinSum Set

The minsum point(s) are:

[xxx.x.] MolossusVar1c1

[xxx.x.] MolossusVar1c1

The minsum distance is: 18

Dataset 6 - Directed Swap MinMax Set

The minmax point(s) are:

[x.xxx.] Choriamb

[xxx.x.] MolossusVar1c1

[xxx.x.] MolossusVar1c1

[.xx.x.] MolossusVar1d1

[.xx.x.] MolossusVar1d1

The minmax distance is: 3

Dataset 6 - Directed Swap MinSum

The minsum point(s) are:

[xxx.x.] MolossusVar1c1

The minsum distance is: 18

Dataset 6 - Directed Swap MinMax

The minmax point(s) are:
[.xx.x.] MolossusVar1d1
[x..xx.] Rhythm not found in database...
[x..x..x] Rhythm not found in database...
[x..x.x.] Rhythm not found in database...
[x..xxx.] Choriamb
[xx..x.] Rhythm not found in database...
[xxx..x.] MolossusVar1c1
The minmax distance is: 3

Dataset 7 - Hamming MinSum Set

The minsum point(s) are:
[x..x.x..x..x..] The6_8ClaveSon
[x..x.x..x..x..] The6_8ClaveSon
The minsum distance is: 11

Dataset 7 - Hamming MinMax Set

The minmax point(s) are:
[x..x.x..x..xx.] The6_8ClaveSonVar2
The minmax distance is: 6

Dataset 7 - Hamming MinSum

The minsum point(s) are:
[x..x.x..x..x..] The6_8ClaveSon
The minsum distance is: 11

Dataset 7 - Hamming MinMax

The minmax point(s) are:
[x..x.....] Rhythm not found in database...
[x..x.....x.] Rhythm not found in database...
[x..x.....xx] Rhythm not found in database...
[x..x.....xx.] Rhythm not found in database...
[x..x.....x...] Rhythm not found in database...
[x..x.....x..x] Rhythm not found in database...
[x..x.....xx] Rhythm not found in database...
[x..x.....xx..] Rhythm not found in database...
[x..x.....xxx.] Rhythm not found in database...
[x..x.....xxxx] Rhythm not found in database...
[x..x.....x..x.] Seguiriya
[x..x.....xx..] Rhythm not found in database...
[x..x.....xx..x.] Rhythm not found in database...
[x..x.....xx..xx] Rhythm not found in database...
[x..x.....xxxx..] Rhythm not found in database...

[x.x.x.x.....] Rhythm not found in database...
[x.x.x.x....x] Rhythm not found in database...
[x.x.x.x...xx] Rhythm not found in database...
[x.x.x.x...x..] Rhythm not found in database...
[x.x.x.x...xx.] Rhythm not found in database...
[x.x.x.x...xxx] Rhythm not found in database...
[x.x.x.x...xx..] Rhythm not found in database...
[x.x.x.x...xx.x] Soli
[x.x.x.x...xxxx] Rhythm not found in database...
[x.x.x.xx....] Rhythm not found in database...
[x.x.x.xx...x..] Rhythm not found in database...
[x.x.x.xx...xx] Rhythm not found in database...
[x.x.x.xx...xx.] Asaadua
[x.x.x...xxx...] Rhythm not found in database...
[x.x.x...xxx..x] Rhythm not found in database...
[x.x.x...xxx.xx] Rhythm not found in database...
[x.x.x...xxxx..] Rhythm not found in database...
[x.x.x...xxxxx..] Rhythm not found in database...
[x.x.x...xxxxxx] Rhythm not found in database...
[x.x.xx....x..] Rhythm not found in database...
[x.x.xx...x....] Rhythm not found in database...
[x.x.xx...xxx..] Rhythm not found in database...
[x.x.xx...xx..x] Rhythm not found in database...
[x.x...xxx.....] Rhythm not found in database...
[x.x...xxx...xx..] Rhythm not found in database...
[x.x...xxx...xx..] Rhythm not found in database...
[x.x...xxx...xx..x] Rhythm not found in database...
[x.x...xxxx...x..] Rhythm not found in database...
[x.x...xxxxx...x..] Rhythm not found in database...
[x.x...xxxxxx...x..] Rhythm not found in database...
[x...xxx.....] Rhythm not found in database...
[x...xxx.....x..] Rhythm not found in database...
[x...xxx.....xx..] Rhythm not found in database...
[x...xxx.....x..x..] Rhythm not found in database...
[x...xxx.....xx..x..] Rhythm not found in database...
[x...xxx.....xxx..] Rhythm not found in database...
[x...xxx.....xx..x..] Rhythm not found in database...
[x...xxx.....xxxx..] Rhythm not found in database...
[x...xxx...x....] Rhythm not found in database...
[x...xxx...x...x..] Rhythm not found in database...
[x...xxx...x...xx..] Rhythm not found in database...
[x...xxx...xx....] Rhythm not found in database...
[x...xxx...xx...x..] Rhythm not found in database...
[x...xxx...xx...xx..] Rhythm not found in database...
[x...xxx...xx...x..x..] Rhythm not found in database...
[x...xxx...xxxx..] Rhythm not found in database...
[x...xxx...xxxxx..] Rhythm not found in database...
[x...xxx...xxxxxx..] Rhythm not found in database...
[x...xxx...xxxxxx..x..] Rhythm not found in database...

[x.xxx.x..x.] Rhythm not found in database...
[x.xxx.x..xxx] Rhythm not found in database...
[x.xxx.xx....] Rhythm not found in database...
[x.xxx.xx...x] Rhythm not found in database...
[x.xxx.xx..xx] Rhythm not found in database...
[x.xxx.xx.x..] Rhythm not found in database...
[x.xxx.xx.xx.] Rhythm not found in database...
[x.xxx.xx.xxx] Rhythm not found in database...
[x.xxx.xxxx..] Rhythm not found in database...
[x.xxx.xxxx.x] Rhythm not found in database...
[x.xxx.xxxxxx] Rhythm not found in database...
[xxxxx.....] Rhythm not found in database...
[xxxxx...xx.] Rhythm not found in database...
[xxxxx..xx..] Rhythm not found in database...
[xxxxx.x..x.] Rhythm not found in database...
[xxxxx.xx...] Rhythm not found in database...
[xxxxx.xxxx.] Rhythm not found in database...
[xxxxxx..x..] Rhythm not found in database...
[xxxxxxx....] Rhythm not found in database...
[xxxxxxx.xx.] Rhythm not found in database...
[xxxxxxxxxx..] Rhythm not found in database...
[xxx.x.....] Rhythm not found in database...
[xxx.x.....x] Rhythm not found in database...
[xxx.x....xx] Rhythm not found in database...
[xxx.x....x..] Rhythm not found in database...
[xxx.x....xx.] Rhythm not found in database...
[xxx.x....xxx] Rhythm not found in database...
[xxx.x...xx..] Rhythm not found in database...
[xxx.x...xx.x] Rhythm not found in database...
[xxx.x...xxxx] Rhythm not found in database...
[xxx.x...xxxxx] Rhythm not found in database...
[xxx.x...xxx..] Rhythm not found in database...
[xxx.x...xx..x] Rhythm not found in database...
[xxx.x..x.xx.] Rhythm not found in database...
[xxx.x..xx...] Rhythm not found in database...
[xxx.x..xx..x] Rhythm not found in database...
[xxx.x..xx.xx] Rhythm not found in database...
[xxx.x...xxx..] Rhythm not found in database...
[xxx.x...xxxx.] Rhythm not found in database...
[xxx.x...xxxxx] Rhythm not found in database...
[xxx.x...xxxxx] Rhythm not found in database...
[xxx.x...xxx..] Rhythm not found in database...
[xxx.x...xx..x] Rhythm not found in database...
[xxx.x...xx...x] Rhythm not found in database...
[xxx.x...xx...xx] Rhythm not found in database...
[xxx.x...xx..xx] Rhythm not found in database...
[xxx.x...xx.x..] Rhythm not found in database...
[xxx.x...xx.xx.] Rhythm not found in database...
[xxx.x...xx.xx..] Rhythm not found in database...
[xxx.x...xx...xx] Rhythm not found in database...
[xxx.x...xx...xx] Rhythm not found in database...
[xxx.x...xx...xx] Rhythm not found in database...
[xxx.x...xx...xx]

```
[xxx.xxxxxx..] Rhythm not found in database...
[xxx.x.xxxxxx.] Rhythm not found in database...
[xxx.x.xxxxxxx] Rhythm not found in database...
[xxx.xx.....] Rhythm not found in database...
[xxx.xx...xx.] Rhythm not found in database...
[xxx.xx...xx..] Rhythm not found in database...
[xxx.xx.x...x.] Rhythm not found in database...
[xxx.xx.xx...] Rhythm not found in database...
[xxx.xx.xxxx.] Rhythm not found in database...
[xxx.xxx...x..] Rhythm not found in database...
[xxx.xxxx....] Rhythm not found in database...
[xxx.xxxx.xx.] Rhythm not found in database...
[xxx.xxxxxxx..] Rhythm not found in database...
[xxxxx....x..] Rhythm not found in database...
[xxxxx....xx] Rhythm not found in database...
[xxxxx...x....] Rhythm not found in database...
[xxxxx...x...x] Rhythm not found in database...
[xxxxx...x.x..] Rhythm not found in database...
[xxxxx...x.xx.] Rhythm not found in database...
[xxxxx...x.xxx] Rhythm not found in database...
[xxxxx...xxx..] Rhythm not found in database...
[xxxxx...xxx.x] Rhythm not found in database...
[xxxxx..xxxxx] Rhythm not found in database...
[xxxxx.xx.x..] Rhythm not found in database...
[xxxxx.xx.x.x] Rhythm not found in database...
[xxxxx.xx.xxx] Rhythm not found in database...
[xxxxx....x..] Rhythm not found in database...
[xxxxx....xx] Rhythm not found in database...
[xxxxx.x....] Rhythm not found in database...
[xxxxx.x.xx.] Rhythm not found in database...
[xxxxx.xxx..] Rhythm not found in database...
[xxxxxx....x..] Rhythm not found in database...
The minmax distance is: 5
```

Dataset 7 - Directed Swap MinSum Set

```
The minsum point(s) are:
[x.x.x..x.xx.] The6_8ClaveSonVar2
The minsum distance is: 9
```

Dataset 7 - Directed Swap MinMax Set

```
The minmax point(s) are:
[x.x.x..x.xx.] The6_8ClaveSonVar2
The minmax distance is: 4
```

Dataset 7 - Directed Swap MinSum

```
The minsum point(s) are:  
[x.x.x..x.xx.] The6_8ClaveSonVar2  
The minsum distance is: 9
```

```
Dataset 7 - Directed Swap MinMax
```

```
-----  
The minmax point(s) are:  
[x.x.x..xx.x.] Rhythm not found in database...  
[x.x.x.x..xx.] Rhythm not found in database...  
[x.xxx..x.xx.] Rhythm not found in database...  
The minmax distance is: 3
```