

**Problem 4. Option II: Axioms and Models**

Consider the following axiom system:

Undefined term: *points*.

Definition: Let  $X$  be a set of points, a certain subset of  $X$  is called *line*.

Definition: Two lines that have no points in common are said to be *parallel*. Axioms:

1. There exists at least one point and at least one line.
2. If  $X$  and  $Y$  are two distinct points, there is a unique line containing them both.
3. Through a given point not on a given line, there is a unique line parallel to the given line.
4. Not all points are on the same line.

Questions:

- a) Say which lines are parallel in each of the figures and give a reason for your answer.
- b) Which of the figures below is a model for this axiom system? Justify your answer.

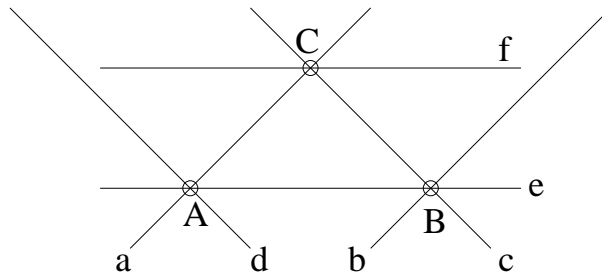


Figure 1: Points are represented as little circles in this figure. If something is not a circle, it's not a point! Points are labeled with capital letters, lines with lowercase letters. For example, line  $c$  consists exactly of points  $B$  and  $C$ . Lines cannot be extended!

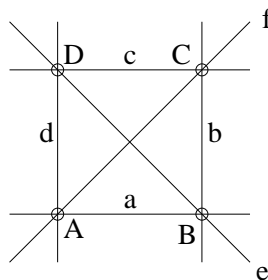


Figure 2: Points are represented as little circles in this figure. If something is not a circle, it's not a point! Points are labeled with capital letters, lines with lowercase letters. Lines cannot be extended!