# Compiler Design

Lecture 4: Automatic Lexer Generation (EaC§2.4)

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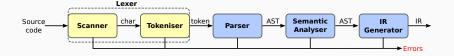
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### **Automatic Lexer Generation**



Starting from a collection of regular expressions (RE) we can automatically generate a Lexer.

Idea: use a Finite State Automata (FSA) for the construction.

# Finite State Automata for Regular

**Expression** 

# Finite State Automata for Regular Expression

Finite State Automata

### **Definition: Finite State Automata**

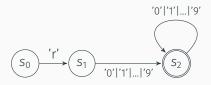
A finite state automata is defined by:

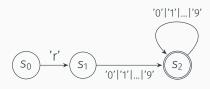
- S, a finite set of states
- $\cdot$   $\Sigma$ , an alphabet, or character set used by the recogniser
- $\delta(s,c)$ , a transition function (takes a state and a character as input, and returns new state)
- $\cdot$  s<sub>0</sub>, the initial or start state
- $S_F$ , a set of final states (a stream of characters is accepted iif the automata ends up in a final state)

### Finite State Automata for Regular Expression

# **Example: register names**register ::= 'r' ('0'|'1'|...|'9') ('0'|'1'|...|'9')\*

The RE (Regular Expression) corresponds to a recogniser (or finite state automata):





### Finite State Automata (FSA) operation:

- Start in state s<sub>0</sub> and take transitions on each input character
- The FSA accepts a word  $\mathbf{x}$  iff  $\mathbf{x}$  leaves it in a final state ( $s_2$ )

### Examples:

- r17 takes it through  $s_0, s_1, s_2$  and accepts
- **r** takes it through  $s_0, s_1$  and fails
- $\cdot$  a starts in  $s_0$  and leads straight to failure

# Table encoding and skeleton code

### To be useful a recogniser must be turned into code



### Table encoding RE

	δ	'r'	'0' '1'  '9'	others
	S <sub>0</sub>	S <sub>1</sub>	error	error
	S <sub>1</sub>	error	S <sub>2</sub>	error
Ī	S <sub>2</sub>	error	S <sub>2</sub>	error

## Skeleton recogniser

```
c = next character state = s_0 while (c \neq EOF) state = \delta(state, c) c = next character if (state final) return success else return error
```

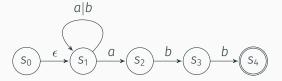
# Finite State Automata for Regular Expression

Non-determinism

### **Deterministic Finite Automaton**

Each RE corresponds to a Deterministic Finite Automaton (DFA). However, it might be hard to construct directly.

What about an RE such as (a|b)\*abb?



#### This is a little different:

- $s_0$  has a transition on  $\epsilon$ , which can be followed without consuming an input character
- s<sub>1</sub> has two transitions on a
- This is a Non-determinisitic Finite Automaton (NFA)

### Non-deterministic vs deterministic finite automata

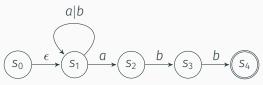
### Deterministic finite state automata (DFA):

- All edges leaving the same node have distinct labels
- There is no  $\epsilon$  transition

### Non-deterministic finite state automata (NFA):

- · Can have multiple edges with same label leaving the same node
- Can have  $\epsilon$  transition
- · This means we might have to backtrack

### Backtracking example for a NFA: input = aabb



From Regular Expression to

**Generated Lexer** 

### **Automatic Lexer Generation**

It is possible to systematically generate a lexer for any regular expression.

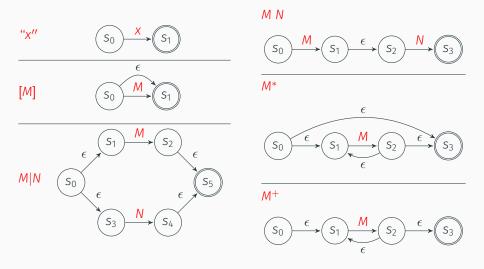
This can be done in three steps:

- 1. regular expression (RE)  $\rightarrow$  non-deterministic finite automata (NFA)
- 2. NFA  $\rightarrow$  deterministic finite automata (DFA)
- 3. DFA  $\rightarrow$  generated lexer

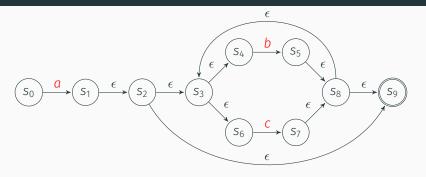
# From Regular Expression to Generated Lexer

Regular Expression to NFA

# 1st step: RE $\rightarrow$ NFA (Ken Thompson, CACM, 1968)



# **Example:** $a(b|c)^*$





(automatic minimization possible)

# From Regular Expression to Generated Lexer

From NFA to DFA

### Step 2: NFA $\rightarrow$ DFA

Executing a non-deterministic finite automata requires backtracking, which is inefficient. To overcome this, we want to construct a DFA from the NFA.

#### The main idea:

- We build a DFA which has one state for each set of states the NFA could end up in.
- A set of state is final in the DFA if it contains the final state from the NFA.
- Since the number of states in the NFA is finite (*n*), the number of possible sets of states (*i.e.* powerset) is also finite:
  - · maximum 2<sup>n</sup> (hint: set encoded as binary vectors)

Assuming the state of the NFA are labelled  $s_i$  and the states of the DFA we are building are labelled  $q_i$ .

We have two key functions:

- reachable( $s_i$ ,  $\alpha$ ) returns the set of states reachable from  $s_i$  by consuming character  $\alpha$
- $\epsilon$ -closure( $s_i$ ) returns the set of states reachable from  $s_i$  by  $\epsilon$  (e.g. without consuming a character)

### The Subset Construction algorithm (Fixed point iteration)

```
q_0 = \epsilon\text{-}closure(s_0); \ Q = \{q_0\}; \ \text{add} \ q_0 \ \text{to WorkList} while (WorkList not empty) remove q from WorkList for each \alpha \in \Sigma subset = \epsilon\text{-}closure(reachable(q,\alpha)) \delta(q,\alpha) = subset if (subset \notin Q) then add subset to Q and to WorkList
```

### The algorithm (in English)

- Start from start state  $s_0$  of the NFA, compute its  $\epsilon$ -closure
- Build subset from all states reachable from  $q_0$  for character  $\alpha$
- Add this subset to the transition table/function  $\delta$
- · If the subset has not been seen before, add it to the worklist
- · Iterate until no new subset are created

### Informal proof of termination

- Q contains no duplicates (test before adding)
- · similarly we will never add twice the same subset to the worklist
- bounded number of states; maximum  $2^n$  subsets, where n is number of state in NFA

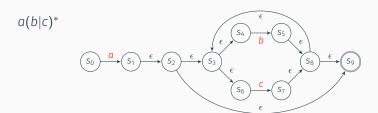
### $\Rightarrow$ the loop halts

#### End result

- · S contains all the reachable NFA states
- It tries each symbol in each s<sub>i</sub>
- · It builds every possible NFA configuration

#### $\Rightarrow$ O and $\delta$ form the DFA

## $\mathsf{NFA} \to \mathsf{DFA}$



		$\epsilon$ -clos	sure(reachable(	$q, \alpha))$
	NFA states	a	b	С
90	S <sub>0</sub>	<i>q</i> <sub>1</sub>	none	none
91	$S_1, S_2, S_3,$	none	<b>q</b> <sub>2</sub>	<i>q</i> <sub>3</sub>
	S <sub>4</sub> , S <sub>6</sub> , S <sub>9</sub>			
$q_2$	S <sub>5</sub> , S <sub>8</sub> , S <sub>9</sub> ,	none	<b>q</b> <sub>2</sub>	<i>q</i> <sub>3</sub>
	S <sub>3</sub> , S <sub>4</sub> , S <sub>6</sub>			
<b>q</b> <sub>3</sub>	S <sub>7</sub> , S <sub>8</sub> , S <sub>9</sub> , S <sub>3</sub> , S <sub>4</sub> , S <sub>6</sub>	none	<b>q</b> <sub>2</sub>	<i>q</i> <sub>3</sub>
	s <sub>3</sub> , s <sub>4</sub> , s <sub>6</sub>			

# Resulting DFA for $a(b|c)^*$

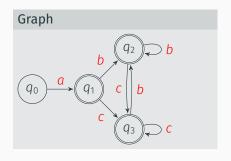


Table encoding					
	a	b	С		
90	91	error	error		
91	error	<b>q</b> <sub>2</sub>	<b>q</b> <sub>3</sub>		
92	error	92	<b>9</b> 3		
<b>q</b> <sub>3</sub>	error	92	<b>q</b> <sub>3</sub>		

- · Smaller than the NFA
- · All transitions are deterministic (no need to backtrack!)
- Could be even smaller (see EaC§2.4.4 Hopcroft's Algorithm for minimal DFA)
- · Can generate the lexer using skeleton recogniser seen earlier

# Final Remarks

### What can be so hard?

### Language design choice can complicate lexing:

- PL/I does not have reserved words (keywords):
   if (cond) then then = else; else else = then
   where are the variables?
- In Fortran & Algol68 blanks (whitespaces) are insignificant:
   do 10 i = 1,25 ≅ do 10 i = 1,25 (loop, 10 is statement label)
   do 10 i = 1,25 ≅ do10i = 1,25 (assignment)
- In C,C++,Java string constants can have special characters: newline, tab, quote, comment delimiters, . . .

### Good language design makes lexing simpler:

e.g. identifier cannot start with a digit in most modern languages
 ⇒ when we see a digit, it can only be the start of a number!

### What does a C lexer sees?

```
u24; // identifier u24
24; // signed number 24
24u; // unsigned number 24
```

# **Building Lexer**

### The important point:

- · All this technology lets us automate lexer construction
- · Implementer writes down regular expressions
- · Lexer generator builds NFA, DFA and then writes out code
- · This reliable process produces fast and robust lexers

### For most modern language features, this works:

- As a language designer you should think twice before introducing a feature that defeats a DFA-based lexer
- The ones we have seen (e.g. insignificant blanks, non-reserved keywords) have not proven particularly useful or long lasting

# Lexer generators input

```
Example: ANSI-C grammar for tokens
https://www.cs.mcgill.ca/~cs520/2022/resources/
ANSI-C-grammar-l.html

For instance:
("["|" <:") { count(); return('['); }</pre>
```

### Next lecture

### Parsing:

- · Context-Free Grammars
- Dealing with ambiguity
- · Recursive descent parser