

# Compiler design

## Lecture 6: Bottom-Up Parsing

---

Christophe Dubach

Winter 2022

Timestamp: 2022/01/17 13:55:13

## Top-Down Parser

A Top-Down parser builds a derivation by working from the start symbol to the input sentence.



## Bottom-Up Parser

A Bottom-Up parser builds a derivation by working from the input sentence back to the start symbol.



# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing

abcde

# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing

abcde

aAbcde

# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing

abcde

aAbcde

aAde

# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing

abcde

aAbcde

aAde

aABe

# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing

abcde

aAbcde

aAde

aABe

Goal

# Bottom-Up Parser

## Example: CFG

Goal ::= a A B e

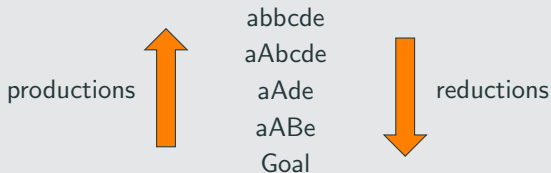
A ::= A b c

A ::= b

B ::= d

Input: abcde

## Bottom-Up Parsing



Note that the production follows a rightmost derivation.



## Leftmost vs Rightmost derivation

---

# Leftmost vs Rightmost derivation

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

## Leftmost derivation

Goal

aABe

aAbcBe

abbcBe

abbcede

LL parsers

## Rightmost derivation

Goal

aABe

aAde

aAbcde

abbcede

LR parsers

# Shift-Reduce Parser

---

# Shift-reduce parser

- It consists of a stack and the input
- It uses four actions:
  1. **shift**: next symbol is shifted onto the stack
  2. **reduce**: pop the symbols  $Y_n, \dots, Y_1$  from the stack that form the right member of a production  $X ::= Y_n, \dots, Y_1$
  3. **accept**: stop parsing and report success
  4. **error**: error reporting routine

## How does the parser know when to shift or when to reduce?

Similarly to a top-down parser, could back-track if wrong decision made or look ahead to decide.

Can build a DFA to decide when we should shift or reduce (will not see it in this course).

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:

## Input

abbcde

## Stack

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation: shift

## Input

bbcde

## Stack

a

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation: shift

## Input

bcde

## Stack

ab

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:

### Input

bcde

### Stack

ab

## Choice here: shift or reduce?

Can lookahead one symbol to make decision.

(Knowing what to do is not explain here, need to analyse the grammar, see EaC§3.5)



# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation: reduce

## Input

bcde

## Stack

aA

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation: shift

## Input

cde

## Stack

aAb

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:

### Input

cde

### Stack

aAb

## Choice here: shift or reduce?

Can lookahead one symbol to make decision.

(Knowing what to do is not explain here, need to analyse the grammar, see EaC§3.5)

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:     shift

## Input

de

## Stack

aAbc

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:        reduce

## Input

de

## Stack

aA

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:        shift

## Input

e

## Stack

aAd

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:            reduce

## Input

e

## Stack

aAB

# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:            shift

**Input**

**Stack**

aABe



# Shift-reduce parser

## Example: CFG

Goal ::= a A B e

A ::= A b c | b

B ::= d

Operation:            reduce

**Input**

**Stack**

Goal

# Top-Down vs Bottom-Up Parsing

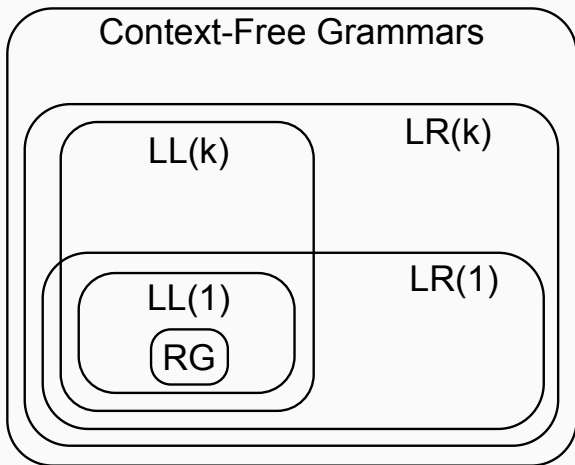
## Top-Down

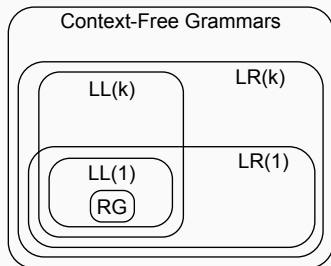
- 👍 Easy to write by hand
- 👍 Easy to integrate with the compiler
- 👎 Supports a smaller class of grammars
  - ⇒ cannot handle left recursion in the grammar
- 👎 Recursion might lead to performance issues
  - 👍 Table encoding possible for better performance

## Bottom-Up

- 👍 Very efficient (no recursion)
- 👍 Supports a larger class of grammar
  - Handles left/right recursion in the grammar
- 👎 Harder to write by hand
  - ⇒ Requires generation tools
- 👎 Rigid integration to compiler

## Expressive Power of Grammars





## Language $\neq$ Grammar

- A language can be defined by more than one grammar
- These grammars might be of different “complexity” (LL(1), LL(k), LR(k))
- $\Rightarrow$  Language complexity  $\neq$  grammar complexity

- Parse tree and abstract syntax tree