#### Compiler Design

Lecture 19: Instruction Selection via Tree-pattern matching

Christophe Dubach Winter 2022

#### (EaC-11.3)

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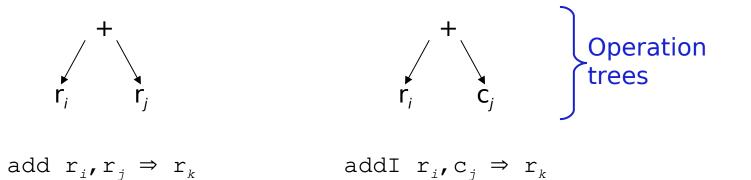
# The Concept

Many compilers use tree-structured IRs

- Abstract syntax trees generated in the parser
- Trees or DAGs for expressions

These systems might well use trees to represent target ISA

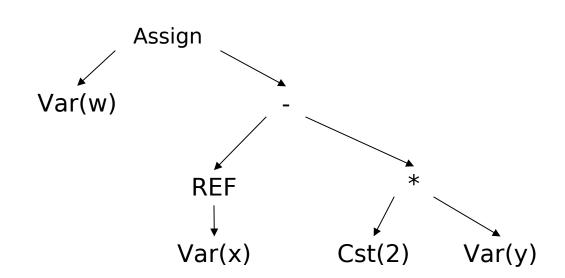
Consider the add operators

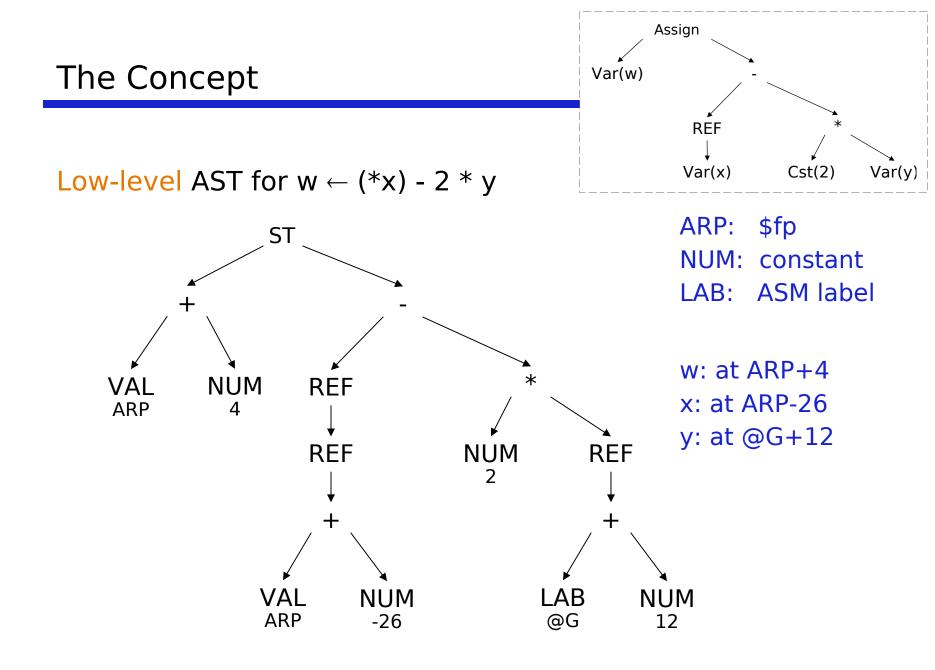


What if we could match these "pattern trees" against IR tree?

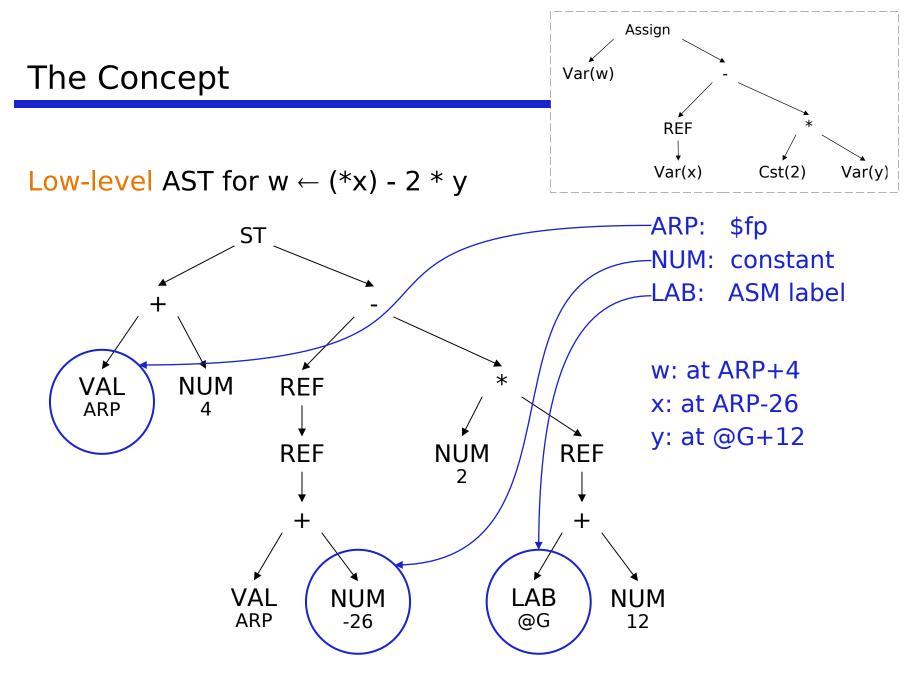
#### The Concept

AST for  $w \leftarrow (*x) - 2 * y$ 





ARP = Activation Record Pointer = **frame pointer** 

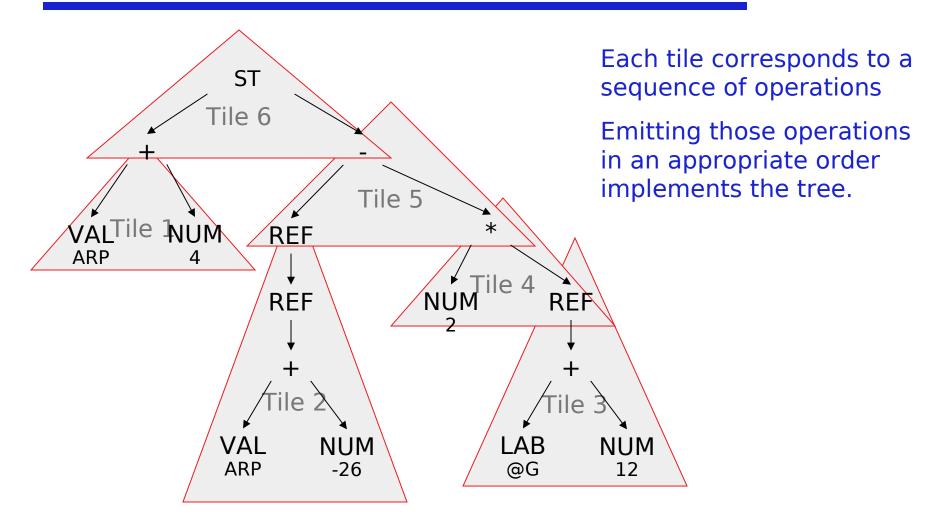


ARP = Activation Record Pointer = **frame pointer** 

#### Tree-pattern matching

Goal is to "tile" AST with operation trees

- A tiling is collection of <ast,op > pairs
  - → *ast* is a node in the low-level AST
  - $\rightarrow$  op is an operation tree
  - $\rightarrow$  *<ast, op >* means that *op* could implement the subtree at *ast*
- A tiling 'implements" an AST if it covers every node in the AST and the overlap between any two trees is limited to a single node
  - →  $<ast, op> \in$  tiling means AST is also covered by a leaf in another operation tree in the tiling, unless it is the root
  - → Where two operation trees meet, they must be compatible (expect the value in the same location)



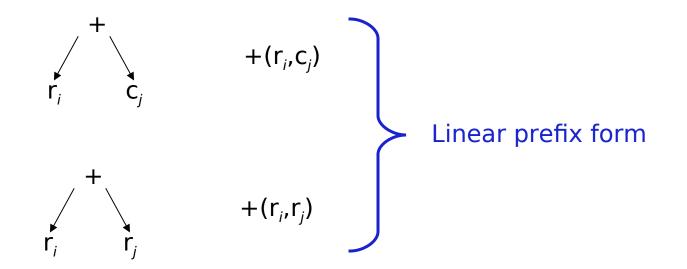
# Generating Code

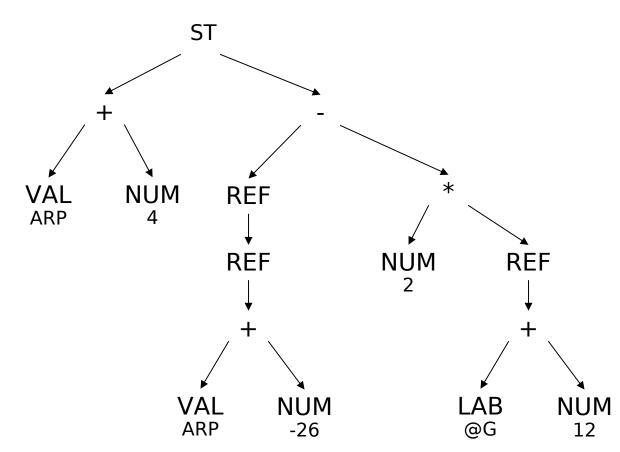
Given a tiled tree

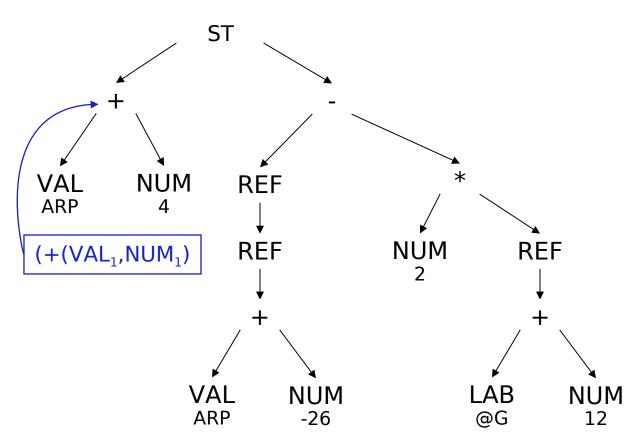
- Postorder treewalk, with node-dependent order for children
  - → Right child of  $\leftarrow$  before its left child
  - → Might impose "most demanding first" rule ...
- Emit code sequence for tiles, in order
- Tie boundaries together with register names
  - $\rightarrow$  Tile 6 uses registers produced by tiles 1 & 5
  - → Tile 6 emits "store  $r_{tile 5} \Rightarrow r_{tile 1}$ "
  - → Can incorporate a "real" register allocator or just use virtual registers

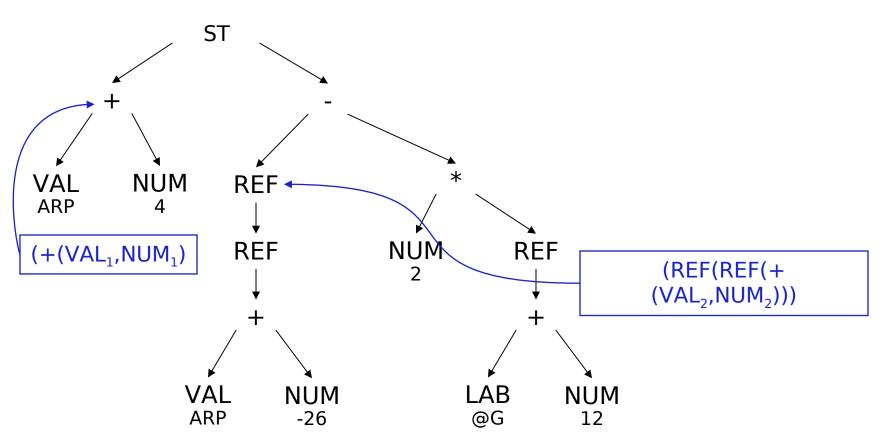
Finding the matches to tile the tree

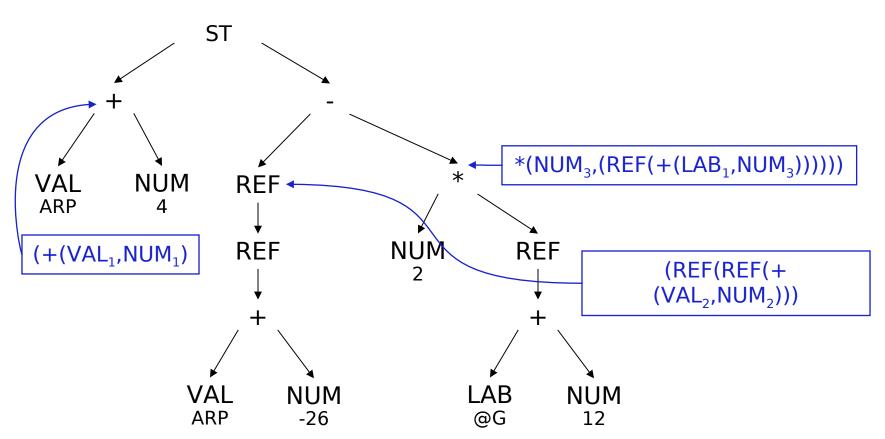
- Compiler writer connects operation trees to AST subtrees
  - $\rightarrow$  Encode tree syntax, in linear form
  - → Provides a set of rewrite rules
  - $\rightarrow$  Associated with each is a code template

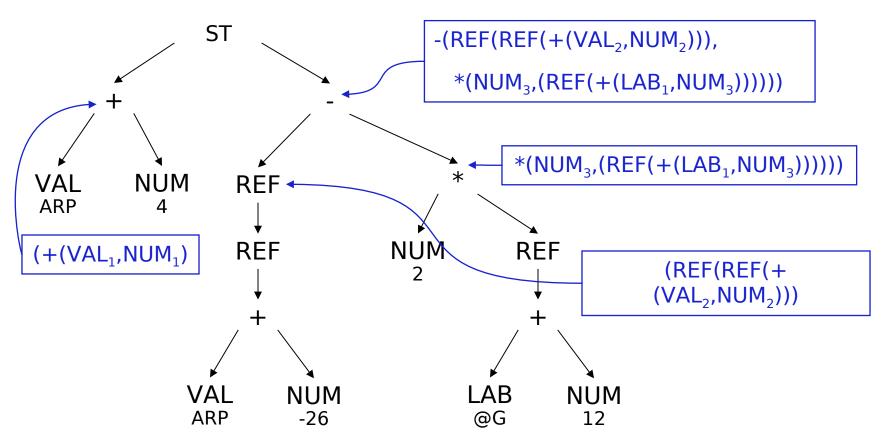


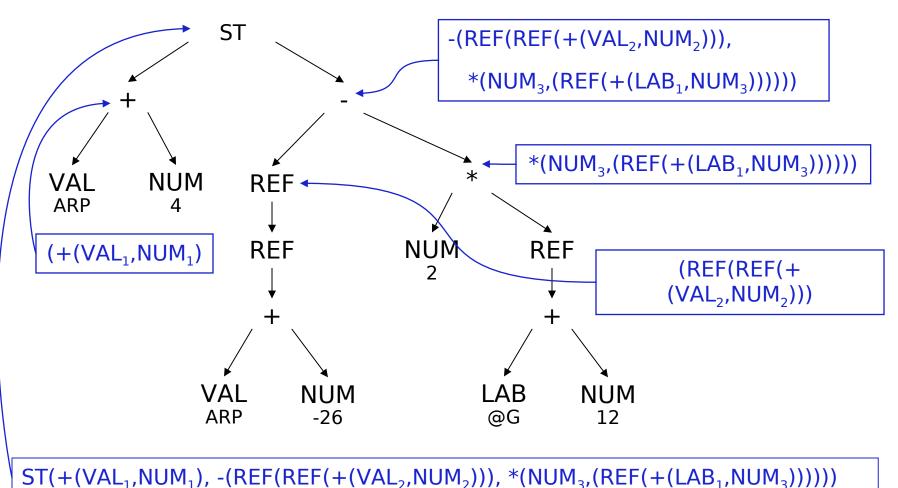












### Rewrite rules: LL Integer AST into ILOC

	Rule	Cost	Template
1	$Goal \rightarrow Assign$	0	
2	Assign $\rightarrow$ ST(Reg <sub>1</sub> ,Reg <sub>2</sub> )	1	store $r_2 \Rightarrow r_1$
3	Assign $\rightarrow$ ST(+(Reg <sub>1</sub> ,Reg <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAO $r_3 \Rightarrow r_1, r_2$
4	Assign $\rightarrow$ ST(+(Reg <sub>1</sub> ,NUM <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_1, n_2$
5	Assign $\rightarrow$ ST(+(NUM <sub>1</sub> ,Reg <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_2, n_1$
6	$Reg \rightarrow LAB_1$	1	loadI $l_1 \Rightarrow r_{new}$
7	$Reg \to VAL_1$	0	
8	$Reg \rightarrow NUM_1$	1	loadI $n_1 \Rightarrow r_{new}$
9	$Reg \to REF(Reg_1)$	1	load $r_1 \Rightarrow r_{new}$
10	$Reg \to REF(+ (Reg_1, Reg_2))$	1	loadAO $r_1, r_2 \Rightarrow r_{new}$
11	$Reg \to REF(+ (Reg_1, NUM_2))$	1	loadAI $r_1, n_2 \Rightarrow r_{new}$
12	$Reg \to REF(+ (NUM_1, Reg_2))$	1	loadAI $r_2, n_1 \Rightarrow r_{new}$

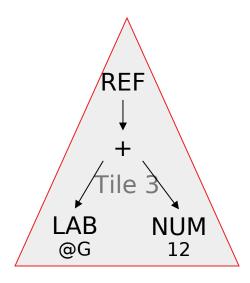
# Rewrite rules: LL Integer AST into ILOC (part II)

	Rule	Cost	Template
13	$Reg \to REF(+ (Reg_1, Lab_2))$	1	loadAI $r_1, l_2 \Rightarrow r_{new}$
14	$Reg \rightarrow REF(+ (Lab_1, Reg_2))$	1	loadAI $r_2, l_1 \Rightarrow r_{new}$
15	$Reg \to + (Reg_1, Reg_2)$	1	addI $r_1, r_2 \Rightarrow r_{new}$
16	$Reg \to + (Reg_1, NUM_2)$	1	addI $r_1, n_2 \Rightarrow r_{new}$
17	$Reg \to + (NUM_1, Reg_2)$	1	addI $r_2, n_1 \Rightarrow r_{new}$
18	$Reg \to + (Reg_1, Lab_2)$	1	addI $r_1, l_2 \Rightarrow r_{new}$
19	$Reg \to + (Lab_1, Reg_2)$	1	addI $r_2, l_1 \Rightarrow r_{new}$
20	$Reg \to - (NUM_1, Reg_2)$	1	rsubl $r_2, n_1 \Rightarrow r_{new}$

A real set of rules would cover more than signed integers ...

Need an algorithm to AST subtrees with the rules

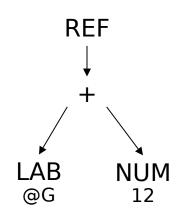
Consider tile 3 in our example



Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

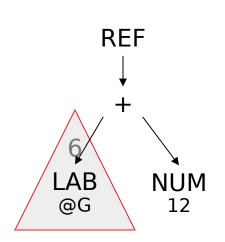
What rules match tile 3?



Need an algorithm to AST subtrees with the rules

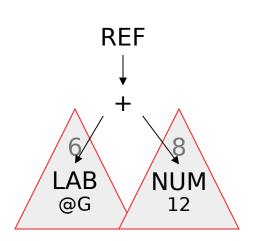
Consider tile 3 in our example

What rules match tile 3? 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node



Need an algorithm to AST subtrees with the rules

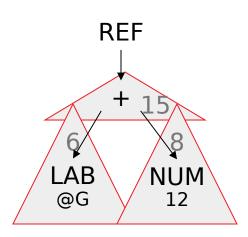
Consider tile 3 in our example



What rules match tile 3? 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node 8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

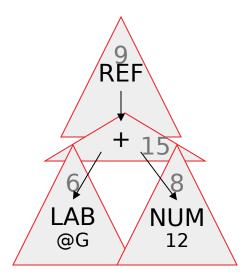


#### What rules match tile 3?

- 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node
- 8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node
- 15:  $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$  tiles the + node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

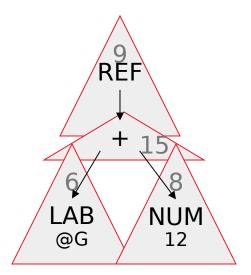


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- 6: Reg  $\rightarrow$  LAB<sub>1</sub> tiles the lower left node
- 8: Reg  $\rightarrow$  NUM<sub>1</sub> tiles the bottom right node
- 15:  $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$  tiles the + node
- 9:  $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$  tiles the REF

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example



#### What rules match tile 3?

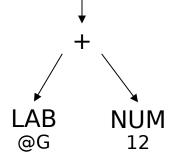
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- 15:  $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$  tiles the + node
- 9:  $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$  tiles the REF

We denote this match as <6,8,15,9> Of course, it implies <8,6,15,9> Both have a cost of 4

# Finding matches

#### Many Sequences Match Our Subtree

Cost	Sequences			
2	6,11	8,14		
3	6,8,10	8,6,10	6,16,9	8,19,9
4	6,8,15,9	8,6,15,9		



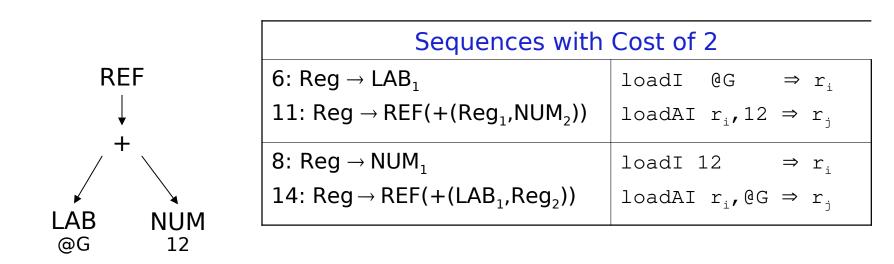
REF

In general, we want the low cost sequence

- Each unit of cost is an operation (1 cycle)
- We should favour short sequences

# Finding matches

#### Low Cost Matches

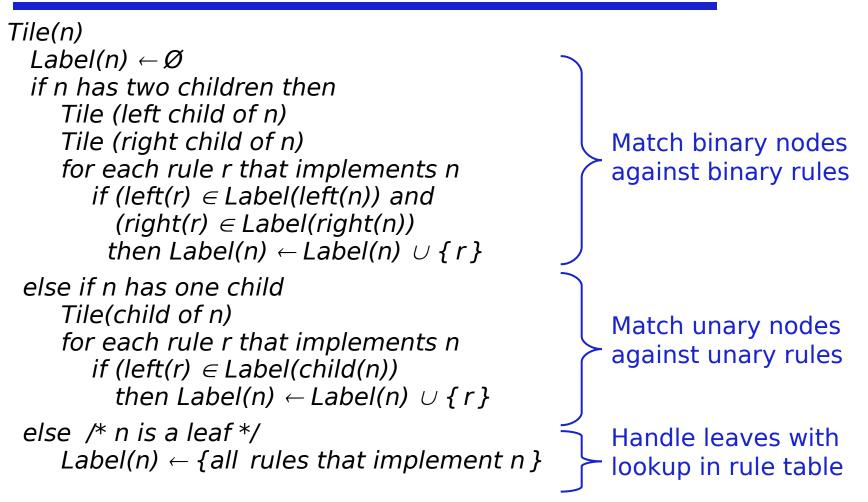


These two are equivalent in cost

6,11 might be better, because @G may be longer than the immediate field

Still need an algorithm

- Assume each rule implements one operator
- Assume operator takes 0, 1, or 2 operands Now, ...



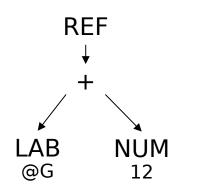
Notes:

- left and right refer to the children of the AST node or right-hand sides of a rule
- implements: e.g. rule 9 implements REF

 $\begin{array}{l} \text{Tile}(n) \\ \text{Label}(n) \leftarrow \varnothing \\ \text{if } n \text{ has two children then} \\ \text{Tile (left child of } n) \\ \text{Tile (right child of } n) \\ \text{for each rule } r \text{ that implements } n \\ \text{if (left}(r) \in \text{Label}(\text{left}(n)) \text{ and} \\ (right(r) \in \text{Label}(right(n)) \\ \text{then Label}(n) \leftarrow \text{Label}(n) \cup \{ \ r \ \} \end{array}$ 

else if n has one child Tile(child of n) for each rule r that implements n if (left(r)  $\in$  Label(child(n)) then Label(n)  $\leftarrow$  Label(n)  $\cup$  { r }

else /\* n is a leaf \*/ Label(n)  $\leftarrow$  {all rules that implement n }



	Rule	\$	Template
1	$\text{Goal} \rightarrow \text{Assign}$	0	
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4	Assign → ST(+ (Reg <sub>1</sub> ,NUM <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_1, n_2$
5	Assign → ST(+ (NUM <sub>1</sub> ,Reg <sub>2</sub> ),Reg <sub>3</sub> )	1	storeAI $r_3 \Rightarrow r_2, n_1$
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20	$Reg \to \text{-} (NUM_1, Reg_2)$	1	rsubl $r_2, n_1 \Rightarrow r_{new}$

Label(Ref) =

- Label(+) =
- Label(Lab) =
- Label(Num) =

```
Tile(n)
 Label(n) \leftarrow Ø
 if n has two children then
    Tile (left child of n)
    Tile (right child of n)
    for each rule r that implements n
       if (left(r) \in Label(left(n))) and
         (right(r) \in Label(right(n)))
        then Label(n) \leftarrow Label(n) \cup { r }
else if n has one child
    Tile(child of n)
    for each rule r that implements n
       if (left(r) \in Label(child(n))
         then Label(n) \leftarrow Label(n) \cup { r }
else /* n is a leaf */
    Label(n) \leftarrow {all rules that implement n }
```

#### This algorithm

- Finds all matches in rule set
- Labels node n with that set

 Can keep lowest cost match at each point for each type of nodes
 → Dynamic programming

 Spends its time in the two matching loops

# The Big Picture

- Tree patterns represent AST and ASM
- Can use matching algorithms to find low-cost tiling of AST
- Can turn a tiling into code using templates for matched rules
- Techniques (& tools) exist to do this efficiently

Hand-coded matcher like Tile	Avoids large sparse table Lots of work
Encode matching as an automaton	O(1) cost per node Tools like BURS (bottom-up rewriting system), BURG
Use parsing techniques	Uses known technology Very ambiguous grammars
Linearize tree into string and use string searching algorithm (Aho- Corasick)	Finds all matches

• Object Oriented Programming Support