

# Compiler Design

## Lecture 10: Semantic Analysis: part II Types

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# Type Systems

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# Type Systems

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## Specification

# What are types used for?

Checking that identifiers are declared and used correctly is not the only thing that needs to be verified in the compiler.

In most programming languages, **expressions have a type**.

Types are here to ensure that expressions are compatible with one another to guarantee some level of correctness.

MY NEW LANGUAGE IS GREAT, BUT IT HAS A FEW QUIRKS REGARDING TYPE:

```
[1] > 2 + "2"
=> "4"
[2] > "2" + []
=> "[2]"
[3] > (2/0)
=> NaN
[4] > (2/0)+2
=> NaN
[5] > "" + ""
=> " + "
[6] > [1,2,3]+2
=> FALSE
[7] > [1,2,3]+4
=> TRUE
[8] > 2/(2-(3/2+1/2))
=> NaN.0000000000000013
[9] > RANGE(" ")
=> (" ", " ", " ", " ", " ")
[10] > + 2
=> 12
[11] > 2+2
=> DONE
[14] > RANGE(1,5)
=> (1,4,3,4,5)
[13] > FLOOR(10.5)
=> |
=> |
=> |
=> |____10.5____
```

source: <https://skod.com/1837/> (CC BY-NC 2.5)

## Examples: typing rules of our Mini-C language

- The operands of `+` must be integers
- The operands of `==` must be compatible (int with int, char with char)
- The number of arguments passed to a function must be equal to the number of parameters
- ...

# Type Systems

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Type properties

# Typing properties

## Strong/weak typing

A language is said to be **strongly typed** if the violation of a typing rule results in an error.

A language is said to be **weakly typed** or not typed in other cases — in particular if the program behaviour becomes unspecified after an incorrect typing.

Strong/weak typing is about **how strictly** types are distinguished (e.g. implicit conversion).



# Typing properties

## Strong/weak typing

A language is said to be **strongly typed** if the violation of a typing rule results in an error.

A language is said to be **weakly typed** or not typed in other cases — in particular if the program behaviour becomes unspecified after an incorrect typing.

Strong/weak typing is about **how strictly** types are distinguished (e.g. implicit conversion).

## Static/dynamic typing

A language is said to be **statically typed** if there exists a type system that can detect incorrect programs before execution.

A language is said to be **dynamically types** in other cases.

Static/dynamic typing is about **when** type information is available

⚠️ A strongly typed language does not imply static typing. ⚠️

## Language examples

	<b>strong</b>	<b>weak</b>
<b>static</b>	Java	C/C++
<b>dynamic</b>	Python	JavaScript

⚠️ A strongly typed language does not imply static typing. ⚠️

## Language examples

	strong	weak
static	Java	C/C++
dynamic	Python	JavaScript

Java (static/strong)

```
class A {}  
class B {}  
A a = (A) b;  
// compile-time error
```

C (static/weak)

```
int * p1;  
char ** p2;  
p1 = (int*) p2;  
// no error
```

Python (dynamic/strong)

```
1+'a'  
# run-time error
```

JavaScript (dynamic/weak)

```
3 + '6'; // '36'  
3 * '6'; // 18  
  
num = 11;  
num.toUpperCase();  
// run-time error
```

Weak dynamic typing: the worst of the worst!

## JavaScript

```
num = 11;  
num.toUpperCase();  
// run-time error
```

```
3 + '6'; // '36'  
3 * '6'; // 18  
// no error
```



source: <http://gusshoecomic.com/648>

We want to give an exact specification of the language.

- We will **formally** define this, using a mathematical notation.
- Programs who pass the type checking phase are **well-typed** since they corresponds to programs for which is it possible to give a **type** to each expression.

This mathematical description will fully specify the typing rules of our language.

# Inference Rules

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Suppose that we have a small language expressing constants (integer literal), the + binary operation and the type **int**.

### Example: language for arithmetic expressions

Constants	$i = a \text{ number (integer literal)}$
Expressions	$e = i$
	$\mid e_1 + e_2$
Types	$T = \mathbf{int}$

# Inference Rules

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## Inference Rules



An expression  $e$  is of type  $T$  iff:

- it's an expression of the form  $i$  and  $T = \mathbf{int}$  or
- it's an expression of the form  $e_1 + e_2$ , where  $e_1$  and  $e_2$  are two expressions of type  $\mathbf{int}$  and  $T = \mathbf{int}$

To represent such a definition, it is convenient to use **inference rules** which in this context is called a **typing rule**:

### Typing rules

$$\text{INTLIT} \frac{}{\vdash i : \mathbf{int}} \qquad \text{BINOP} \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## Typing rules

$$\text{INTLIT} \frac{}{\vdash i : \text{int}}$$

$$\text{BINOP} \frac{\vdash e_1 : \text{int} \quad \vdash e_2 : \text{int}}{\vdash e_1 + e_2 : \text{int}}$$

An inference rule is composed of:

- a horizontal **line**
- a **name** on the left or right of the line
- a list of **premisses** placed above the line
- a **conclusion** placed below the line

An inference rule where the list of premisses is empty is called an **axiom**.

An inference rule can be read bottom up:

### Example

$$\text{BINOP} \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

“To show that an expression of the form  $e_1 + e_2$  has type **int**, we need to show that  $e_1$  and  $e_2$  have the type **int**”.

- To show that the conclusion of a rule holds, it is enough to prove that the premisses are correct
- This process stops when we encounter an axiom.

Using the inference rule representation, it possible to see whether an expression is well-typed.

**Example: (1+2)+3**

$$\text{BINOP} \frac{\text{BINOP} \frac{\text{INTLIT} \frac{}{\vdash 1 : \text{int}} \quad \text{INTLIT} \frac{}{\vdash 2 : \text{int}}}{\vdash 1 + 2 : \text{int}} \quad \text{INTLIT} \frac{}{\vdash 3 : \text{int}}}{\vdash (1 + 2) + 3 : \text{int}}}$$

Using the inference rule representation, it possible to see whether an expression is well-typed.

### Example: $(1+2)+3$

$$\text{BINOP} \frac{\text{BINOP} \frac{\text{INTLIT} \frac{}{\vdash 1 : \text{int}} \quad \text{INTLIT} \frac{}{\vdash 2 : \text{int}}}{\vdash 1 + 2 : \text{int}} \quad \text{INTLIT} \frac{}{\vdash 3 : \text{int}}}{\vdash (1 + 2) + 3 : \text{int}}}$$

Such a tree is called a **derivation tree**.

### Conclusion

An expression  $e$  has type  $T$  iff there exist a derivation tree whose conclusion is  $\vdash e : T$ .

# Inference Rules

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## Environments

# Identifiers

Let's add identifiers to our language.

## Example: language for arithmetic expressions

Identifiers	$x = a \text{ name (string literal)}$
Constants	$i = a \text{ number (integer literal)}$
Expressions	$e = i$ $\quad   \quad e_1 + e_2$ $\quad   \quad x$
Types	$T = \mathbf{int}$

To determine if an expression such as  $x+1$  is well-typed, we need to have information about the type of  $x$ .

We add an **environment**  $\Gamma$  to our typing rules which associates a type for each identifier. We now write  $\Gamma \vdash e : T$ .

# Environment

An typing environment  $\Gamma$  is list of pairs of an identifier  $x$  and a type  $T$ .  
We can add an inference rule to decide when an expression containing an identifier is well-typed:

$$\text{IDENT} \frac{x : T \in \Gamma}{\Gamma \vdash x : T}$$



# Environment

An typing environment  $\Gamma$  is list of pairs of an identifier  $x$  and a type  $T$ .  
We can add an inference rule to decide when an expression containing an identifier is well-typed:

$$\text{IDENT} \frac{x : T \in \Gamma}{\Gamma \vdash x : T}$$

## Example: $x + 1$

In the environment  $\Gamma = \{x : \mathbf{int}\}$ , it is possible to type check  $x + 1$

$$\text{BINOP} \frac{\text{IDENT} \frac{x : \mathbf{int} \in \Gamma}{\Gamma \vdash x : \mathbf{int}} \quad \text{INTLIT} \frac{}{\Gamma \vdash 1 : \mathbf{int}}}{\Gamma \vdash x + 1 : \mathbf{int}}$$

# Inference Rules

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## Function Call

# Function call

We need to add a notation to talk about the type of the functions.

## Example: language for arithmetic expressions

Identifiers      $x = a \text{ name (string literal)}$

Constants        $i = a \text{ number (integer literal)}$

Expressions      $e = i$   
                  |  $e_1 + e_2$   
                  |  $x$

Types             $T, U = \mathbf{int}$   
                  |  $(U_1, \dots, U_n) \rightarrow T$

where  $(U_1, \dots, U_n) \rightarrow T$  represents a function type.

## Function call inference rule

$$\text{FUNCALL}(f) \frac{\Gamma \vdash f : (U_1, \dots, U_n) \rightarrow T \quad \Gamma \vdash x_1 : U_1 \quad \dots \quad \Gamma \vdash x_n : U_n}{\Gamma \vdash f(x_1, \dots, x_n) : T}$$

In plain English:

- each argument  $x_i$  must be of type  $U_i$
- the function  $f$  is defined in the environment  $\Gamma$  as a function taking parameters of types  $U_1, \dots, U_n$  and a return type  $T$ .

## Function call inference rule

$$\text{FUNCALL}(f) \frac{\Gamma \vdash f : (U_1, \dots, U_n) \rightarrow T \quad \Gamma \vdash x_1 : U_1 \quad \dots \quad \Gamma \vdash x_n : U_n}{\Gamma \vdash f(x_1, \dots, x_n) : T}$$

In plain English:

- each argument  $x_i$  must be of type  $U_i$
- the function  $f$  is defined in the environment  $\Gamma$  as a function taking parameters of types  $U_1, \dots, U_n$  and a return type  $T$ .

### Example: `int foo(int, int)`

$$\text{FUNCALL}(\text{foo}) \frac{\Gamma \vdash \text{foo} : (\text{int}, \text{int}) \rightarrow \text{int} \quad \Gamma \vdash x_1 : \text{int} \quad \Gamma \vdash x_2 : \text{int}}{\Gamma \vdash \text{foo}(x_1, x_2) : \text{int}}$$

# Implementation

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# Implementation

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Visitor implementation

$$\text{BINOP}(+) \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {
```



$$\text{BINOP}(+) \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {  
    Type lhsT = bo.lhs.accept(this);  
    Type rhsT = bo.rhs.accept(this);  
}
```

$$\text{BINOP}(+) \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {  
    Type lhsT = bo.lhs.accept(this);  
    Type rhsT = bo.rhs.accept(this);  
    if (bo.op == ADD) {
```

$$\text{BINOP}(+) \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {
    Type lhsT = bo.lhs.accept(this);
    Type rhsT = bo.rhs.accept(this);
    if (bo.op == ADD) {
        if (lhsT == Type.INT && rhsT == Type.INT) {
```

$$\text{BINOP}(+) \frac{\vdash e_1 : \mathbf{int} \quad \vdash e_2 : \mathbf{int}}{\vdash e_1 + e_2 : \mathbf{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {  
    Type lhsT = bo.lhs.accept(this);  
    Type rhsT = bo.rhs.accept(this);  
    if (bo.op == ADD) {  
        if (lhsT == Type.INT && rhsT == Type.INT) {  
            bo.type = Type.INT; // set the type  
        }  
    }  
}
```

$$\text{BINOP}(+) \frac{\vdash e_1 : \text{int} \quad \vdash e_2 : \text{int}}{\vdash e_1 + e_2 : \text{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {
    Type lhsT = bo.lhs.accept(this);
    Type rhsT = bo.rhs.accept(this);
    if (bo.op == ADD) {
        if (lhsT == Type.INT && rhsT == Type.INT) {
            bo.type = Type.INT; // set the type
            return Type.INT;    // returns it
        }
    }
}
```

$$\text{BINOP}(+) \frac{\vdash e_1 : \text{int} \quad \vdash e_2 : \text{int}}{\vdash e_1 + e_2 : \text{int}}$$

## TypeChecker visitor : binary operation

```
public Type visitBinOp(BinOp bo) {
    Type lhsT = bo.lhs.accept(this);
    Type rhsT = bo.rhs.accept(this);
    if (bo.op == ADD) {
        if (lhsT == Type.INT && rhsT == Type.INT) {
            bo.type = Type.INT; // set the type
            return Type.INT;    // returns it
        } else
            error();
    }
    // ...
}
```

## TypeChecker visitor: variables

```
public Type visitVarDecl(VarDecl vd) {  
    if (vd.type == VOID)  
        error();  
    return null;  
}
```

## TypeChecker visitor: variables

```
public Type visitVarDecl(VarDecl vd) {
    if (vd.type == VOID)
        error();
    return null;
}

public Type visitVarExp(Var v) {
    v.type = v.vd.type;
    return v.vd.type;
}
```



## TypeChecker visitor: variables

```
public Type visitVarDecl(VarDecl vd) {
    if (vd.type == VOID)
        error();
    return null;
}

public Type visitVarExp(Var v) {
    v.type = v.vd.type;
    return v.vd.type;
}
```

### Not just analysis!

The visitor does more than analysing the AST: it also remembers the result of the analysis directly in the AST node.

## Exercise: write the visit method for function call

```
public Type visitFunCall(FunCall fc) {  
    // ...  
}
```

## Function call inference rule

$$\text{FUNCALL}(f) \frac{\Gamma \vdash f : (U_1, \dots, U_n) \rightarrow T \quad \Gamma \vdash x_1 : U_1 \quad \dots \quad \Gamma \vdash x_n : U_n}{\Gamma \vdash f(x_1, \dots, x_n) : T}$$

- Typing rules can be formally defined using inference rules.
- We saw how to implement them with a visitor

Next lecture:

- An introduction to Assembly