Lecture 19 Instruction Selection: Tree-pattern matching

(EaC-11.3)

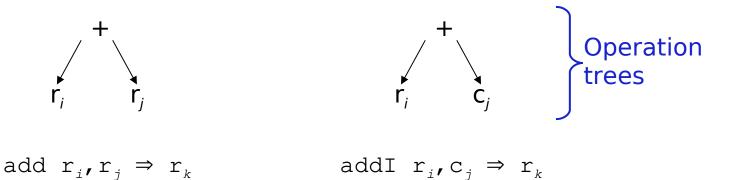
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Many compilers use tree-structured IRs

- Abstract syntax trees generated in the parser
- Trees or DAGs for expressions

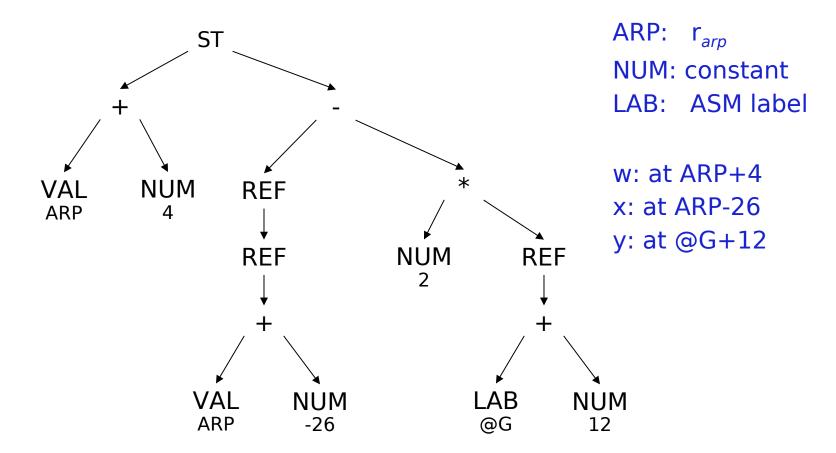
These systems might well use trees to represent target ISA

Consider the add operators



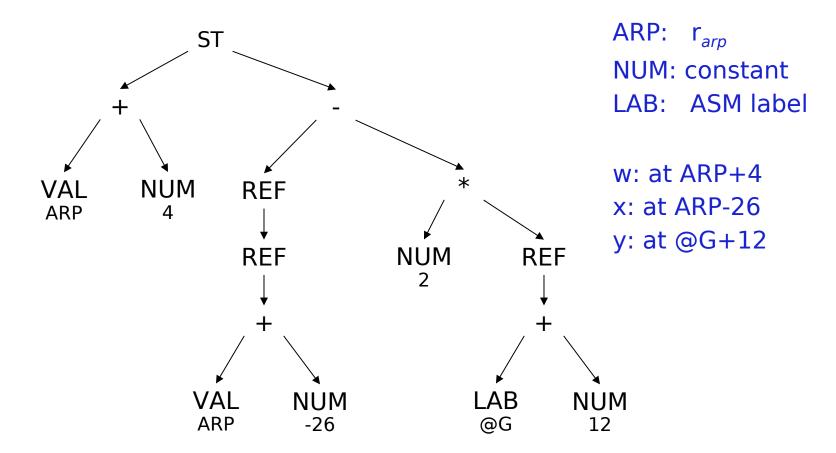
If we can match these "pattern trees" against IR trees, ...

Low-level AST for $w \leftarrow (*x) - 2 * y$

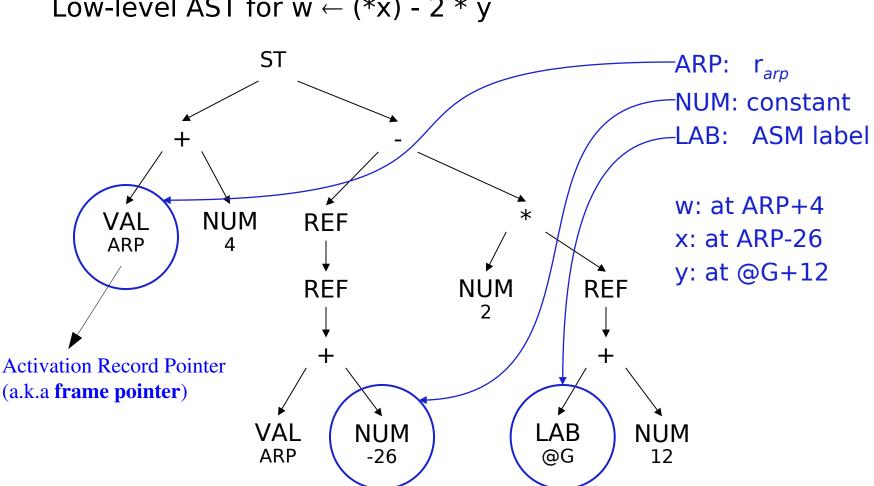


(Ref \approx Load)

Low-level AST for $w \leftarrow (*x) - 2 * y$



(Ref \approx Load)

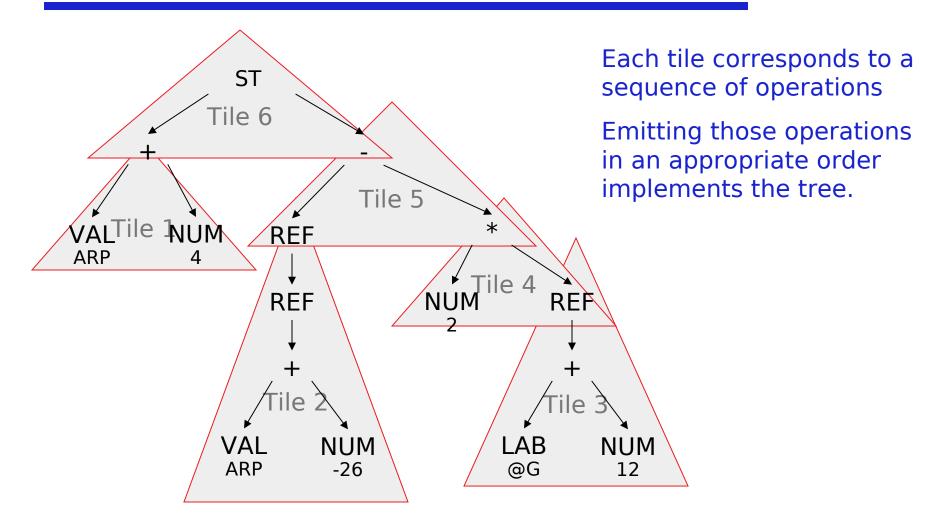


Low-level AST for $w \leftarrow (*x) - 2 * y$

Tree-pattern matching

Goal is to "tile" AST with operation trees

- A tiling is collection of <ast,op > pairs
 - \rightarrow ast is a node in the AST
 - \rightarrow op is an operation tree
 - \rightarrow *<ast, op >* means that *op* could implement the subtree at *ast*
- A tiling 'implements" an AST if it covers every node in the AST and the overlap between any two trees is limited to a single node
 - → $<ast, op> \in$ tiling means *ast* is also covered by a leaf in another operation tree in the tiling, unless it is the root
 - → Where two operation trees meet, they must be compatible (expect the value in the same location)



Generating Code

Given a tiled tree

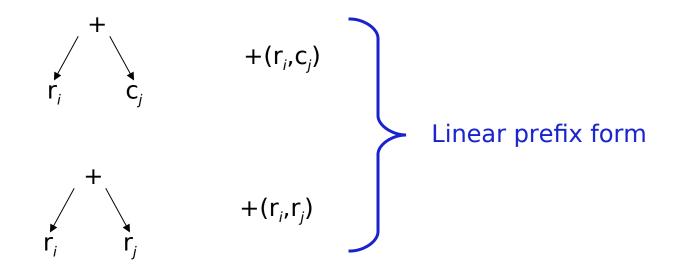
- Postorder treewalk, with node-dependent order for children
 - → Right child of \leftarrow before its left child
 - → Might impose "most demanding first" rule ...
- Emit code sequence for tiles, in order
- Tie boundaries together with register names
 - \rightarrow Tile 6 uses registers produced by tiles 1 & 5
 - → Tile 6 emits "store $r_{tile 5} \Rightarrow r_{tile 1}$ "
 - → Can incorporate a "real" register allocator or just use virtual registers

Finding the matches to tile the tree

- Compiler writer connects operation trees to AST subtrees
 - \rightarrow Encode tree syntax, in linear form
 - → Provides a set of rewrite rules
 - \rightarrow Associated with each is a code template

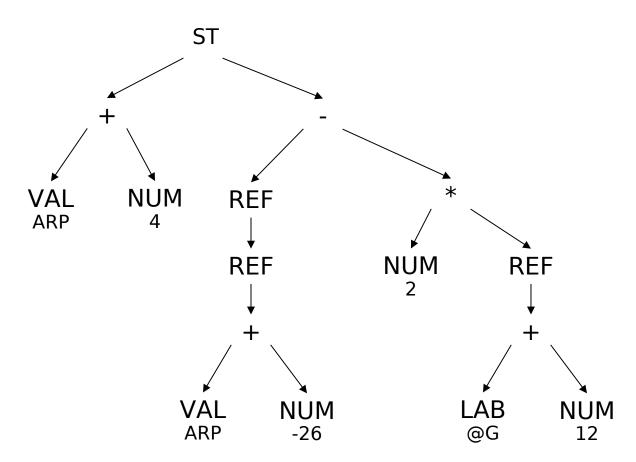
Notation

To describe these trees, we need a concise notation



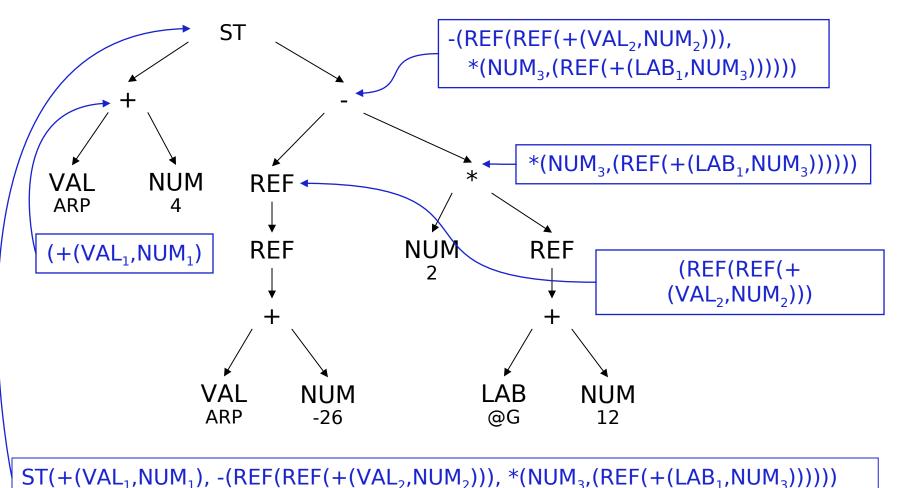
Notation

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Notation

To describe these trees, we need a concise notation



Rewrite rules: LL Integer AST into ILOC

| | Rule | Cost | Template |
|----|---|------|---------------------------------------|
| 1 | $Goal \rightarrow Assign$ | 0 | |
| 2 | Assign \rightarrow ST(Reg ₁ ,Reg ₂) | 1 | store $r_2 \Rightarrow r_1$ |
| 3 | Assign \rightarrow ST(+(Reg ₁ ,Reg ₂),Reg ₃) | 1 | storeAO $r_3 \Rightarrow r_1, r_2$ |
| 4 | Assign \rightarrow ST(+(Reg ₁ ,NUM ₂),Reg ₃) | 1 | storeAI $r_3 \Rightarrow r_1, n_2$ |
| 5 | Assign \rightarrow ST(+(NUM ₁ ,Reg ₂),Reg ₃) | 1 | storeAI $r_3 \Rightarrow r_2, n_1$ |
| 6 | $Reg \rightarrow LAB_1$ | 1 | loadI $l_1 \Rightarrow r_{new}$ |
| 7 | $Reg \to VAL_1$ | 0 | |
| 8 | $Reg \rightarrow NUM_1$ | 1 | loadI $n_1 \Rightarrow r_{new}$ |
| 9 | $Reg \rightarrow REF(Reg_1)$ | 1 | load $r_1 \Rightarrow r_{new}$ |
| 10 | $Reg \to REF(+ (Reg_1, Reg_2))$ | 1 | loadAO $r_1, r_2 \Rightarrow r_{new}$ |
| 11 | $Reg \to REF(+ (Reg_1, NUM_2))$ | 1 | loadAI $r_1, n_2 \Rightarrow r_{new}$ |
| 12 | $\text{Reg} \rightarrow \text{REF}(+ (\text{NUM}_1, \text{Reg}_2))$ | 1 | loadAI $r_2, n_1 \Rightarrow r_{new}$ |

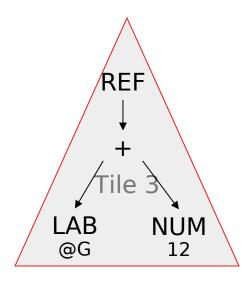
Rewrite rules: LL Integer AST into ILOC (part II)

| | Rule | Cost | Template |
|----|------------------------------------|------|---------------------------------------|
| 13 | $Reg \to REF(+ (Reg_1, Lab_2))$ | 1 | loadAI $r_1, l_2 \Rightarrow r_{new}$ |
| 14 | $Reg \to REF(+ (Lab_1, Reg_2))$ | 1 | loadAI $r_2, l_1 \Rightarrow r_{new}$ |
| 15 | $Reg \to + (Reg_1, Reg_2)$ | 1 | addI $r_1, r_2 \Rightarrow r_{new}$ |
| 16 | $Reg \to + (Reg_1, NUM_2)$ | 1 | addI $r_1, n_2 \Rightarrow r_{new}$ |
| 17 | $Reg \to + (NUM_1, Reg_2)$ | 1 | addI $r_2, n_1 \Rightarrow r_{new}$ |
| 18 | $Reg \to + (Reg_1, Lab_2)$ | 1 | addI $r_1, l_2 \Rightarrow r_{new}$ |
| 19 | $Reg \to + (Lab_1, Reg_2)$ | 1 | addI $r_2, l_1 \Rightarrow r_{new}$ |
| 20 | $Reg \rightarrow - (NUM_1, Reg_2)$ | 1 | rsubl $r_2, n_1 \Rightarrow r_{new}$ |
| | | | |

A real set of rules would cover more than signed integers ...

Need an algorithm to AST subtrees with the rules

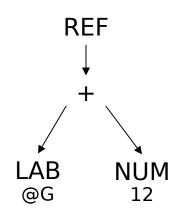
Consider tile 3 in our example



Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

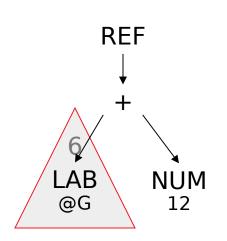
What rules match tile 3?



Need an algorithm to AST subtrees with the rules

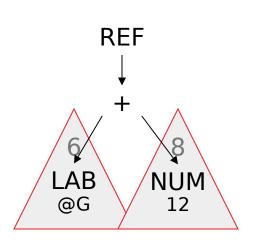
Consider tile 3 in our example

What rules match tile 3? 6: Reg \rightarrow LAB₁ tiles the lower left node



Need an algorithm to AST subtrees with the rules

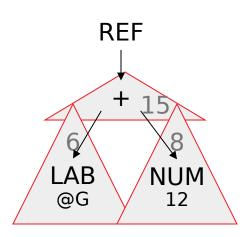
Consider tile 3 in our example



What rules match tile 3? 6: Reg \rightarrow LAB₁ tiles the lower left node 8: Reg \rightarrow NUM₁ tiles the bottom right node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example



What rules match tile 3?

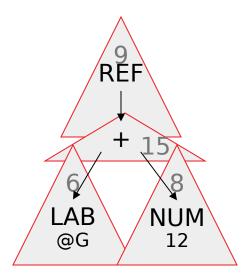
6: Reg \rightarrow LAB₁ tiles the lower left node

8: Reg \rightarrow NUM₁ tiles the bottom right node

15: $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$ tiles the + node

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example

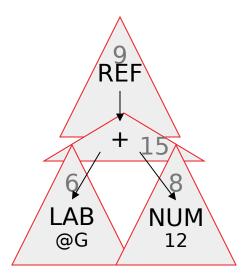


What rules match tile 3?

- 6: Reg \rightarrow LAB₁ tiles the lower left node
- 8: Reg \rightarrow NUM₁ tiles the bottom right node
- 15: $\text{Reg} \rightarrow + (\text{Reg}_1, \text{Reg}_2)$ tiles the + node
- 9: $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$ tiles the REF

Need an algorithm to AST subtrees with the rules

Consider tile 3 in our example



What rules match tile 3?

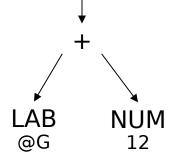
- 6: Reg \rightarrow LAB₁ tiles the lower left node
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- 9: $\text{Reg} \rightarrow \text{REF}(\text{Reg}_1)$ tiles the REF

We denote this match as <6,8,15,9> Of course, it implies <8,6,15,9> Both have a cost of 4

Finding matches

Many Sequences Match Our Subtree

| Cost | Sequences | | | | |
|------|-----------|----------|--------|--------|--|
| 2 | 6,11 | 8,14 | | | |
| 3 | 6,8,10 | 8,6,10 | 6,16,9 | 8,19,9 | |
| 4 | 6,8,15,9 | 8,6,15,9 | | | |



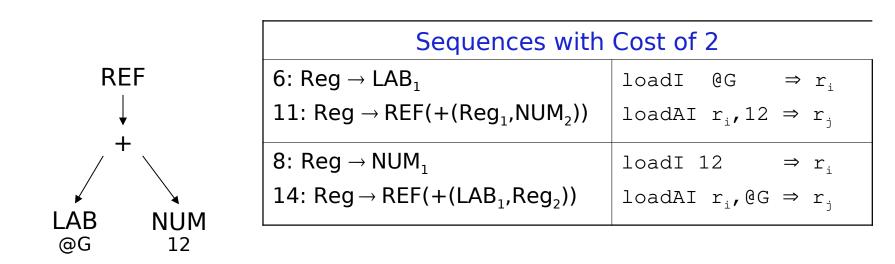
REF

In general, we want the low cost sequence

- Each unit of cost is an operation (1 cycle)
- We should favour short sequences

Finding matches

Low Cost Matches

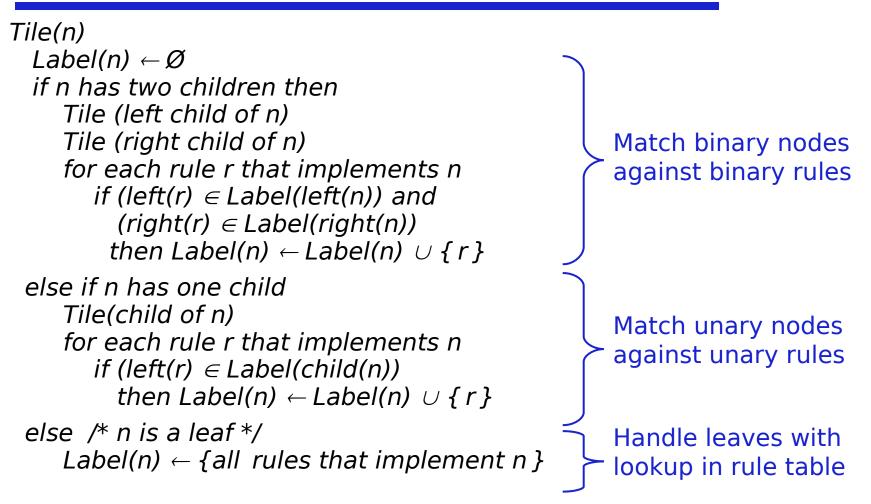


These two are equivalent in cost

6,11 might be better, because @G may be longer than the immediate field

Still need an algorithm

- Assume each rule implements one operator
- Assume operator takes 0, 1, or 2 operands Now, ...



Notes:

- left and right refer to the children of the AST node or right-hand sides of a rule
- implements: e.g. rule 9 implements REF

Tile(n) Label(n) $\leftarrow \emptyset$ if n has two children then Tile (left child of n) Tile (right child of n) for each rule r that implements n if (left(r) \in Label(left(n)) and $(right(r) \in Label(right(n)))$ then Label(n) \leftarrow Label(n) \cup { r } else if n has one child Tile(child of n) for each rule r that implements n if (left(r) \in Label(child(n)) then Label(n) \leftarrow Label(n) \cup { r }

else /* n is a leaf */ Label(n) \leftarrow {all rules that implement n }

This algorithm

- Finds all matches in rule set
- Labels node n with that set
- Can keep lowest cost match at each point
- Leads to a notion of local optimality — lowest cost at each point
- Spends its time in the two matching loops

The Big Picture

- Tree patterns represent AST and ASM
- Can use matching algorithms to find low-cost tiling of AST
- Can turn a tiling into code using templates for matched rules
- Techniques (& tools) exist to do this efficiently

| Hand-coded matcher like Tile | Avoids large sparse table Lots of work |
|--|---|
| Encode matching as an automaton | O(1) cost per node Tools like BURS (bottom- up rewriting system), BURG |
| Use parsing techniques | Uses known technology Very ambiguous grammars |
| Linearize tree into string and use string searching algorithm (Aho-Corasick) | Finds all matches |