Static analysis

*Static analysis* determines interesting properties of programs to enable some optimizations.

All interesting properties are actually undecidable, so the analysis computes a conservative approximation:

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- if we say *yes*, then the property definitely holds;
- if we say *no*, then the property may or may not hold;
- only the *yes* answer will help us to perform the optimization;
- $\bullet\,$ a trivial analysis will sayno always; so
- the art is to say *yes* as often as possible.

Properties need not be simply *yes* or *no*, in which case the notion of *approximation* is more subtle.

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Static analysis (3)

Static analysis may take place:

- at the source code level;
- at some intermediate level; or
- at the machine code level.

Static analysis may look at:

- basic blocks only;
- $\bullet\,$  an entire function (intraprocedural); or
- the whole program (interprocedural).

In each case, we are maximally pessimistic at the boundaries.

The precision and cost of an analysis rises as we include more information.

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Static analysis (4)

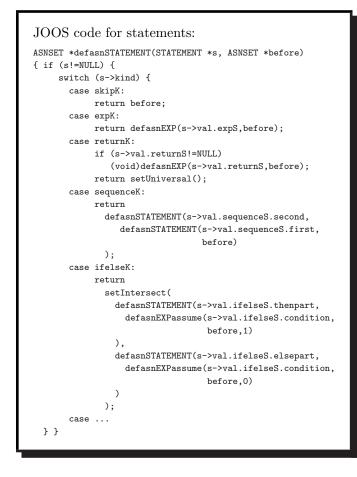
Simple static analysis:

- is merely advanced weeding;
- uses symbol and type information; and
- is recursive in the program syntax.

An example is the *definite assignment* requirement in Java and JOOS:

- local variables must be assigned before they are read;
- this is undecidable; but
- the language specification dictates a specific conservative approximation.

For each program point, compute a set of local variables that: • contains only variables that have definitely been assigned; • may be too small, since the analysis is conservative; and • depends on the set computed for the previous program point. It accepts: { int k: if (flag) k = 3; else k = 4; System.out.println(k); } but rejects: { int k; if (flag) k = 3; if (!flag) k = 4; System.out.println(k); }



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Static analysis (7)

```
To make the analysis more precise, it considers
boolean expressions in more detail.
```

```
The procedure defasnEXPassume(...,b) assumes the expression evalutes to b.
```

This refinement handles a case like:

```
{ int k;
   if (a>0 && (k=b)>0) System.out.println(k);
}
```

which would otherwise be rejected.

In general, a static analysis becomes more precise when it may make further assumptions about the context. COMP 520 Fall 2008

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```
Static analysis (8)
```

The definite assignment analysis is particularly simple:

there are no recursive dependencies between the computed sets.

This allows a simple implementation: a top-down traversal of the parse tree.

For more sophisticated analyses, we generate equations and compute the solution as a fixed point. of registers:

mov 1,R3

mov R3,R1

registers:

is not used later on.

For basic block register allocation, which variables need to be written back to memory?

The naïve scheme:

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• must write all those variables that are *only* in registers.

A better scheme:

• write all those variables that are only in registers *and* whose values might be used later on.

This could avoid many useless spills.

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Static analysis (11)

In both examples, we need to know if some  $R_i$  might be used later on. If so, it is called *live*; otherwise, it is called *dead*.

For the JIT compiler, we want to optimize the use

This requires knowledge about the future uses of

The optimization is only sound if the value of R3

mov 1,R1

A static analysis can conservatively approximate liveness at each program point.

Exact liveness is of course undecidable.

A trivial analysis will call everything live, which precludes all optimizations.

A superior analysis will identify more dead variables.

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Static analysis (12)

Liveness analysis for VirtualRISC:

- build a control flow graph (goto graph);
- define dataflow equations for each node;
- compute the least solution of these equations.

For basic blocks the computation is trivial.

For intraprocedural analysis we must compute a minimal fixed point in a lattice.

mov 3,<u>R1</u> mov 4,<u>R2</u>

add R1,R2,<u>R3</u> mov R3,<u>R0</u> return

Consider a simple basic block:

others are merely read (used).

S2:

S3:

S1: mov 3,R1

S4: mov R3, R0

S5: return

mov 4,R2

add R1,R2,R3

The control flow graph is:

Static analysis (13)

Each instruction uses some registers and defines some registers:

		$\mathrm{uses}(\mathtt{S}_{i})$	$\operatorname{defines}({\tt S}_{\boldsymbol i})$
S1:	mov 3, <u>R1</u>	{}	$\{\texttt{R1}\}$
S2:	↓ mov 4, <u>R2</u>	{}	{R2}
S3:	↓ add R1,R2, <u>R3</u>	{R1,R2}	{R3}
S4:	₩ mov R3, <u>R0</u>	{R3}	{R0}
S5:	<b>↓</b> return	{R0}	{}

The register R0 is implicitly used for the return value.



Static analysis (15)

Let  $out(S_i)$  be the variables that are live just *after*  $S_i$  and  $in(S_i)$  those that are live just *before*  $S_i$ :

The <u>underlined</u> registers are written (defined), the

$$\begin{array}{c|c} & in(S_i) \\ S_i: & op X, Y, Z \\ & out(S_i) \end{array}$$

Then we have the dataflow equation:

```
in(\mathbf{S}_i) = uses(\mathbf{S}_i) \cup (out(\mathbf{S}_i) - defines(\mathbf{S}_i))
```

We add those registers that are used in the current instruction and delete those that are defined here.  ${\rm COMP~520~Fall~2008}$ 

```
Static analysis (16)
```

```
Since out(S5) = \{\}, it follows that:
in(S5) = uses(S5) = \{R0\}
We can continue to unravel the equations:
     out(S4) = in(S5) = \{R0\}
     in(S4) = uses(S4) \cup (out(S4) - defines(S4))
              = \{ \texttt{R3} \} \cup (\{ \texttt{R0} \} - \{ \texttt{R0} \})
              = \{ R3 \}
     out(S3) = in(S4) = \{R3\}
     in(S3) = uses(S3) \cup (out(S3) - defines(S3))
              = \{ \texttt{R1,R2} \} \cup (\{ \texttt{R3} \} - \{ \texttt{R3} \})
              = \{ R1, R2 \}
and so on:
                          uses(S_i)
                                          defines(S_i)
                                                         in(S_i)
S1: mov 3,<u>R1</u>
                          {}
                                          {R1}
                                                         {}
S2: mov 4,<u>R2</u>
                          {}
                                          \{R2\}
                                                         {R1}
S3: add R1,R2,<u>R3</u> {R1,R2}
                                          {R3}
                                                         {R1,R2}
S4: mov R3, R0
                                          {R0}
                                                          {R3}
                          {R3}
S5: return
                          {R0}
                                          {}
                                                          {R0}
```

In basic blocks we use the equation:

$$out(S_i) = in(S_{i+1})$$

If we have branches, then a node in the control flow graph may have several successors.

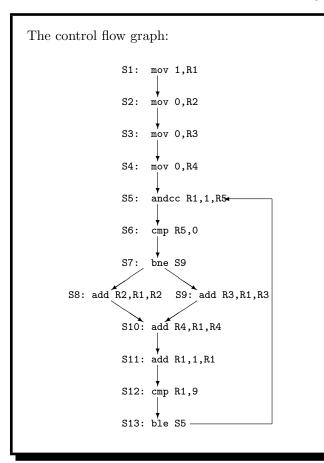
In this case, we must use the equation:

$$\operatorname{out}(\mathtt{S}_i) = \bigcup_{x \in \operatorname{succ}(\mathtt{S}_i)} \operatorname{in}(x)$$

But now the equations are cyclic and cannot simply be unraveled.

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Static analysis (19)



```
Consider the small piece of C code:
{ int i, sum_even, sum_odd, sum;
  i = 1;
  sum_even = 0;
  sum_odd = 0;
  sum = 0;
  while (i < 10)
   { if (i%2 == 0) sum_even = sum_even + i;
     else sum_odd = sum_odd + i;
     sum = sum + i;
     i++;
  }
}
It yields the following VirtualRISC code:
                           // R1 is i
        mov 1,R1
        mov 0,<u>R2</u>
                           // R2 is sum_even
        mov 0,<u>R3</u>
                           // R3 is sum_odd
        mov 0,<u>R4</u>
                           // R4 is sum
loop:
                          // R5 = R1 & 1
        andcc R1,1,<u>R5</u>
        cmp R5,0
                          // if R5 != 0 goto else
        bne else
        add R2,R1,R2
                          // R2 = R2 + R1; even case
        b endif
else:
        add R3,R1,<u>R3</u>
                          // R3 = R3 + R1; odd case
endif:
        add R4,R1,R4
                          // R4 = R4 + R1; update sum
        add R1,1,<u>R1</u>
                          // R1 = R1 + 1; increment i
        cmp R1,9
        ble loop
                          // if i <= 9 goto loop
```

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Static analysis (20)

To unravel the liveness equations, we should start with:

out(S13) = in(S5)

but we have not computed in(S5) yet, so this will not work!

If  $in(S1), \ldots, in(S13)$  are known, then we can unravel the code as before and obtain the sets  $in(S1), \ldots, in(S13)$  once again.

But this means that unraveling is a function:

$$f:\mathcal{P}(R)^{13}
ightarrow\mathcal{P}(R)^{13}$$

where  $R = \{R1, R2, \dots, R5\}$ . A solution is a fixed point, and we want the minimal one.

Two fundamental observations:

• the set  $D = \mathcal{P}(R)^{13}$  is a finite *lattice*:

 $orall x,y\in D:x\sqcap y\in D\ \wedge\ x\sqcup y\in D$ 

where  $\sqsubseteq$  is point-wise set inclusion; and

• the unraveling function f is *monotonic*:

 $\forall x,y \in D: x \sqsubseteq y \Rightarrow f(x) \sqsubseteq f(y)$ 

since  $g(x) = A \cup (x - B)$  is monotonic.

The fixed point theorem:

Any monotonic function f on a finite lattice D has the unique minimal fixed point:

$$\bigsqcup_i f^i(\perp)$$

which is always obtained after finitely many iterations.

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Static analysis (23)

Computing the minimal fixed point:						
	uses	defs	succ		$f(\perp)$	$f^2(\perp)$
S1		R1	S2	{}	{}	{}
S2		R2	S3	{}	{}	{}
S3		R3	S4	{}	{}	{}
S4		R4	S5	{}	{}	{R1}
S5	R1	R5	S6	{}	{R1}	{R1}
S6	R5		S7	{}	{R5}	{R5}
S7			S8,S9	{}	{}	{R1,R2,R3
S8	R1,R2	R2	S10	{}	$\{R1,R2\}$	{R1,R2,R4
S9	R1,R3	R3	S10	{}	$\{ \texttt{R1,R3} \}$	{R1,R3,R4
S10	R1,R4	R4	S11	{}	$\{ \texttt{R1,R4} \}$	{R1,R4}
S11	R1	R1	S12	{}	{R1}	{R1}
S12	R1		S13	{}	{R1}	{R1}
S13			S5	{}	{}	{R1}

The function is:

$$f(X_1, X_2, \dots, X_{13}) = (Y_1, Y_2, \dots, Y_{13})$$

where:

$$Y_i = \mathrm{uses}(\mathtt{S}_i) \cup (igcup_{\mathtt{S}_j} \in \mathrm{succ}(\mathtt{S}_i)) \ \mathtt{S}_j \in \mathrm{succ}(\mathtt{S}_i)$$

For 
$$D = \mathcal{P}(R)^{13}$$
 we have that:

 $\bot = (\emptyset, \emptyset, \dots, \emptyset)$ 

so we start with the sets  $in(S_i) = \{\}$  and keep unraveling until they no longer change.

Note that:

$$au = (R, R, \dots, R)$$

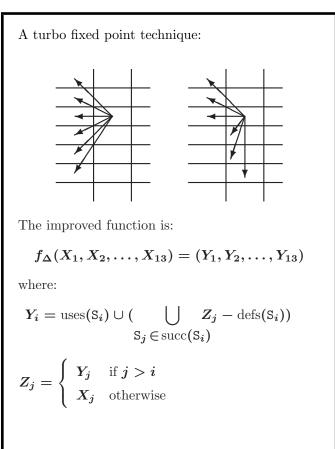
is always a safe answer, but clearly useless and pessimistic.

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Static analysis (24)

	$f^3(\bot)$	$f^4(\perp)$	$f^5(\perp)$
S1	{}	{}	{}
S2	{}	{R1}	{R1}
S3	{R1}	{R1}	{R1}
S4	{R1}	{R1}	${R1,R2,R3}$
S5	{R1}	$\{R1,R2,R3\}$	$\{R1, R2, R3, R4\}$
S6	${R1,R2,R3,R5}$	$\{R1,R2,R3,R4,R5\}$	{R1,R2,R3,R4,R5}
S7	$\{R1,R2,R3,R4\}$	$\{R1,R2,R3,R4\}$	$\{R1,R2,R3,R4\}$
S8	${R1,R2,R4}$	{R1,R2,R4}	{R1,R2,R4}
S9	${R1,R3,R4}$	$\{ \texttt{R1,R3,R4} \}$	$\{R1,R3,R4\}$
S10	{R1,R4}	{R1,R4}	{R1,R4}
S11	{R1}	{R1}	{R1}
S12	{R1}	{R1}	$\{R1,R2,R3\}$
S13	{R1}	$\{R1,R2,R3\}$	$\{R1,R2,R3,R4\}$
	$f^6(\perp)$	$f^7(\perp)$	$f^{8}(\perp)$
S1	{}	{}	{}
S2	(D4)	{R1}	{R1}
52	{R1}		( )
52 S3	{R1,R2}	{R1,R2}	{R1,R2}
	()	{R1,R2} {R1,R2,R3}	{R1,R2} {R1,R2,R3}
S3	{R1,R2}	C . J	C
S3 S4	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4}	{R1,R2,R3}	{R1,R2,R3} {R1,R2,R3,R4}
S3 S4 S5	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4}	{R1,R2,R3} {R1,R2,R3,R4}	{R1,R2,R3} {R1,R2,R3,R4}
S3 S4 S5 S6	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5]
S3 S4 S5 S6 S7	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4}
S3 S4 S5 S6 S7 S8	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R4}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R4}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R3,R4}
S3 S4 S5 S6 S7 S8 S9	{R1,R2} {R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R4} {R1,R3,R4}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R4} {R1,R3,R4}	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R3,R4} {R1,R2,R3,R4}
S3 S4 S5 S6 S7 S8 S9 S10 S11	{R1,R2}         {R1,R2,R3}         {R1,R2,R3,R4}         {R1,R2,R3,R4,R5}         {R1,R2,R3,R4,R5}         {R1,R2,R3,R4}         {R1,R2,R3,R4}         {R1,R2,R3,R4}         {R1,R2,R3,R4}         {R1,R3,R4}         {R1,R3,R4}         {R1,R4}	<pre>{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R4} {R1,R3,R4} {R1,R3,R4} </pre>	{R1,R2,R3} {R1,R2,R3,R4} {R1,R2,R3,R4,R5} {R1,R2,R3,R4,R5} {R1,R2,R3,R4} {R1,R2,R3,R4} {R1,R2,R3,R4} {R1,R2,R3,R4}

Static analysis (25)



Improved fixed point computation:

	$\bot$	$f_\Delta(\perp)$	$f_{\Delta}^2(\perp)$	$f_\Delta^3(\perp)$
S1	{}	{}	{}	{}
S2	{}	{}	{R1}	{R1}
S3	{}	{}	{R1,R2}	{R1,R2}
S4	{}	{}	${R1,R2,R3}$	{R1,R2,R3}
S5	{}	{R1}	$\{R1,R2,R3,R4\}$	{R1,R2,R3,R4}
S6	{}	{R5}	{R1,R2,R3,R4,R5}	{R1,R2,R3,R4,R5}
S7	{}	{}	$\{R1,R2,R3,R4\}$	${R1,R2,R3,R4}$
S8	{}	{R1,R2}	{R1,R2,R4}	$\{R1,R2,R3,R4\}$
S9	{}	{R1,R3}	{R1,R3,R4}	{R1,R2,R3,R4}
S10	{}	{R1,R4}	{R1,R4}	$\{R1,R2,R3,R4\}$
S11	{}	{R1}	{R1}	{R1,R2,R3,R4}
S12	{}	{R1}	{R1}	{R1,R2,R3,R4}
S13	{}	{}	{R1}	{R1,R2,R3,R4}

Number of iterations is down from 8 to 3.

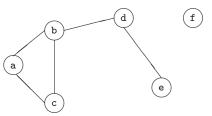
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Static analysis (27)

Liveness analysis is used for register allocation in optimizing compilers.

In the basic block case, reduce spills to those variables that are only in registers *and* live.

In the intraprocedural case, construct a graph whose nodes are variables:



and where edges connect nodes that are live at the same time.

Register allocation is now reduced to finding a minimal graph coloring:

{ {a,d,f}, {b,e}, {c} }

and assigning a register to each color.

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#### Static analysis (28)

Liveness analysis is a *backwards* analysis, since we unravel from the future towards the past.

An example of a *forwards* analysis is constant propagation:

S1:	mov 3,R1	$\{(R0,?),(R1,?),(R2,?),(R3,?)\}$
S2:	↓ mov 4,R2	$\{(R0,?),(R1,3),(R2,?),(R3,?)\}$
S3:	add R1,R2,R3	$\{(R0,?),(R1,3),(R2,4),(R3,?)\}$
S4:	mov R3,R0	$\{(R0,?),(R1,3),(R2,4),(R3,7)\}$
S5:	return	{(R0,7),(R1,3),(R2,4),(R3,7)}

A basic static analysis of JOOS and other object-oriented languages is *type inference*.

Given an expression, what are the possible classes of the objects to which it may evaluate?

The exact answer is undecidable, so we must conservatively approximate:

- we will accept a set that is too large;
- we want it as small as possible; and
- a trivial answer includes all classes.

This analysis is interprocedural and requires access to the whole program.

Possible uses of type inference:

- inline methods when there is only one possible receiver;
- eliminate run-time checks that can be decided statically;
- remove code that is never executed; and
- approximate the control flow graph to enable other static analyses.

In each case, smaller inferred sets will give better results.

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Static analysis (31)

The constraint technique:

- assign a variable [[E]] to each occurrence of an expression E;
- assign a variable [[m]] to each occurrence of a method m;
- the variables range over the set of all classes  $C = \{C_1, C_2, \dots, C_n\};$
- each parse tree node generates a local constraint on the variables; and
- the global minimal solution of these constraints is finally computed.

Again, we must compute a minimal fixed point in a finite lattice.

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#### Static analysis (32)

Each constraint models the flow of objects:

- the assignment "i = E" yields:  $\llbracket E \rrbracket \subseteq \llbracket i \rrbracket$ ;
- the creation "new C()" yields:
   {C} ⊆ [[new C()]];
- the cast "C(E)" yields:
   {C} ⊆ [[C(E)]];
- the constant "this" yields: {C}  $\subseteq [[this]]$ , where C is the surrounding class; and
- the statement "return E" yields: [[E]] ⊆ [[m]], where m is the surrounding method.

The method invocation:

yields the *conditional* constraints:

 $\llbracket E_1 \rrbracket \subseteq \llbracket x_1 \rrbracket$ 

 $C_{i} \in \llbracket E \rrbracket \Rightarrow \begin{cases} \llbracket \mathbf{L} \rrbracket \sqsubseteq \llbracket \mathbf{L} \rrbracket \sqsubseteq \llbracket \mathbf{L} \rrbracket \rrbracket \subseteq \llbracket \mathbf{L} \varUpsilon \rrbracket \rrbracket \\ \vdots \\ \llbracket \mathbf{E}_{k} \rrbracket \subseteq \llbracket \mathbf{L}_{k} \rrbracket \\ \llbracket \mathbf{E}_{k} \rrbracket \subseteq \llbracket \mathbf{L}_{k} \rrbracket \\ \llbracket \mathbf{m} \rrbracket \subseteq \llbracket \mathbf{E} \cdot \mathbf{m} (\mathbf{E}_{1}, \mathbf{E}_{2}, \dots, \mathbf{E}_{k}) \rrbracket \end{cases}$ 

whenever the class  $C_i$  implements a method named **m** which accepts **k** arguments named  $x_1$ ,

 $E.m(E_1, E_2, ..., E_k)$ 

Since the constraint:

 $v\subseteq w$ 

holds if and only if the equality:

 $w=v\cup w$ 

does, we can rewrite a set of constraints into a function:

 $f: \mathcal{P}(C)^k \to \mathcal{P}(C)^k$ 

such that fixed-points of f correspond to solutions to the constraints.

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 $\mathbf{x}_{2}, \ldots, \mathbf{x}_{k}$ .

Static analysis (35)

For the example constraints:

$$egin{aligned} v_1 &\subseteq v_2 \ & \mathbb{C}_3 \in v_2 \Rightarrow v_3 \subseteq v_1 \ & \{\mathbb{C}_7\} \subseteq v_3 \end{aligned}$$

we get the function:

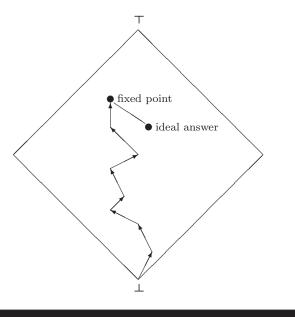
$$\begin{split} f(X_1, X_2, X_3) = \\ \begin{cases} (X_1 \cup X_3, X_1 \cup X_2, \{\mathbb{C}_7\} \cup X_3) & \text{if } \mathbb{C}_3 \in X_2 \\ (X_1, X_1 \cup X_2, \{\mathbb{C}_7\} \cup X_3) & \text{otherwise} \end{cases} \end{split}$$

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Static analysis (36)

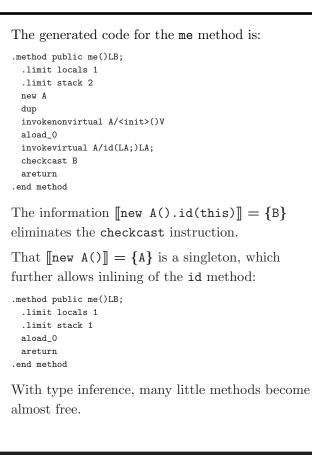
Solving the constraints:

- $\mathcal{P}(C)^k$  is a finite lattice;
- each function f is monotonic; and
- the least fixed point of **f** is the unique smallest solution of the constraints.



Static analysis (37)

```
A tiny JOOS sketch:
public class A {
     public A() { super(); }
     public A id(A x) { return x; }
7
public class B extends A {
     public B() { super(); }
     public B me() { return (B)(new A()).id(this); }
The generated constraints are:
 \begin{matrix} \llbracket \mathtt{x} \rrbracket_A \subseteq \llbracket \mathtt{id} \rrbracket_A \\ \llbracket \mathtt{x} \rrbracket_B \subseteq \llbracket \mathtt{id} \rrbracket_B \\ \end{matrix} 
[\![(B)(\texttt{new A}()).\texttt{id}(\texttt{this})]\!] \subseteq [\![\texttt{me}]\!]
 \{B\} \subseteq [\![(B)(\texttt{new }A()).\texttt{id}(\texttt{this})]\!]
 \{B\} \subseteq \llbracket \text{this} \rrbracket \\ \{A\} \subseteq \llbracket \text{new } A() \rrbracket 
\mathbf{A} \in \llbracket \texttt{new } \mathbf{A}(\texttt{)} \rrbracket \Rightarrow \llbracket \texttt{this} \rrbracket \subseteq \llbracket \texttt{x} \rrbracket_{\mathbf{A}}
\mathsf{A} \in \llbracket \mathsf{new} \ \mathsf{A}() \rrbracket \Rightarrow \llbracket \mathsf{id} \rrbracket_{\mathsf{A}} \subseteq \llbracket (\mathsf{new} \ \mathsf{A}()) \, . \, \mathsf{id}(\mathsf{this}) \rrbracket
B \in \llbracket \text{new A()} \rrbracket \Rightarrow \llbracket \text{this} \rrbracket \subseteq \llbracket x \rrbracket_B
\mathsf{B} \in \llbracket[\texttt{new A}()\rrbracket \Rightarrow \llbracket[\texttt{id}\rrbracket_B \subseteq \llbracket(\texttt{new A}()).\texttt{id}(\texttt{this})\rrbracket
The minimal solution is:
[[new A()]] = \{A\}
\llbracket x \rrbracket_A = \llbracket id \rrbracket_A = \llbracket this \rrbracket = \llbracket (new A()).id(this) \rrbracket = \{B\}\llbracket (B)(new A()).id(this) \rrbracket = \{B\}
[[x]]_B = [[id]]_B = \{\}
```



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Static analysis (39)

Improving analyses by transformations:

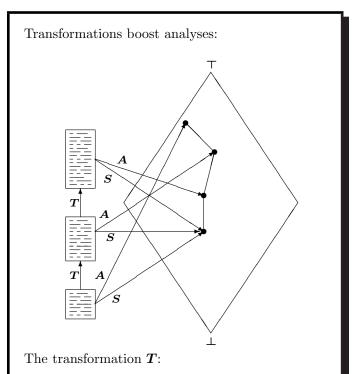
- let **P** be our set of programs;
- let  $S: P \rightarrow D$  be an ideal static analysis (uncomputable); and
- let  $T: P \to P$  be a program transformation that preserves the semantics.

Since S gives the ideal information, clearly S(T(p)) = S(p) for all  $p \in P$ .

However, if  $A : P \to D$  is a conservative approximation to S, then A(T(p)) may be different from A(p), perhaps even better.

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Static analysis (40)



- may unfold the program to make it more explicit; or
- may itself be an optimization.