

# Abstract Syntax Trees

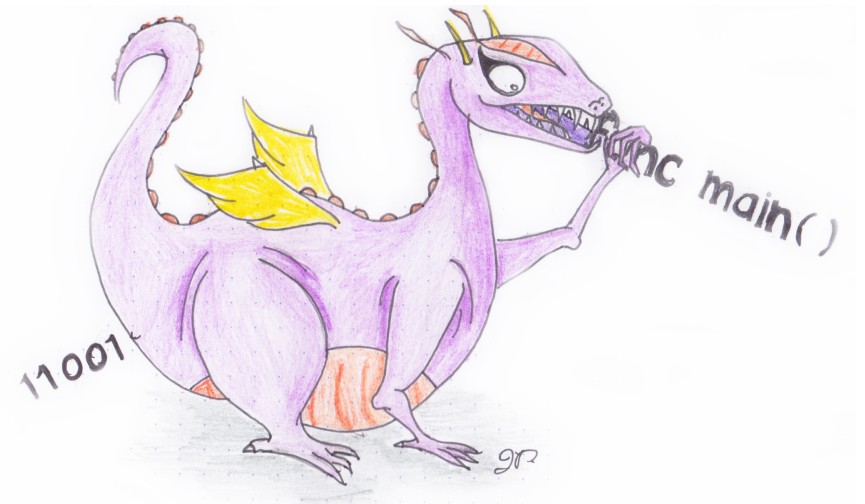
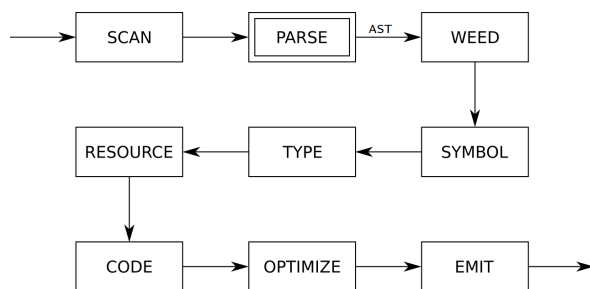
COMP 520: Compiler Design (4 credits)

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MWF 10:30-11:30, TR 1100

<http://www.cs.mcgill.ca/~cs520/2020/>



# Readings

## Crafting a Compiler (recommended)

- Chapter 7

# Announcements (Wednesday/Friday, January 22nd/24th)

## Milestones

- Group signup form <https://forms.gle/HgeCthhH3dwD6WmG7>, fill this out over the next 2 weeks

## Assignment 1

- Questions in a few minutes!
- **Due:** Friday, January 24th 11:59 PM

## Midterm

- **Date:** Tuesday, February 25th from 6:00 - 7:30 PM in RPHYS 112

# Background on Programming Languages - Expressions

An *expression* is a programming language construct which is associated with a *value*. We can define them recursively:

- Base cases
  - Literals: “string”, `true`, `1.0`, ...
  - Identifiers: `a`, `myVar`, ...
- Recursive cases
  - Binary operations: `<Expression> <Op> <Expression>`
  - Unary operations: `<Op> <Expression>`
  - Parentheticals: `(Expression)`
  - Function calls

Note that in the above definitions, we do not specify any *type* information (e.g. `int`, `float`, etc.).

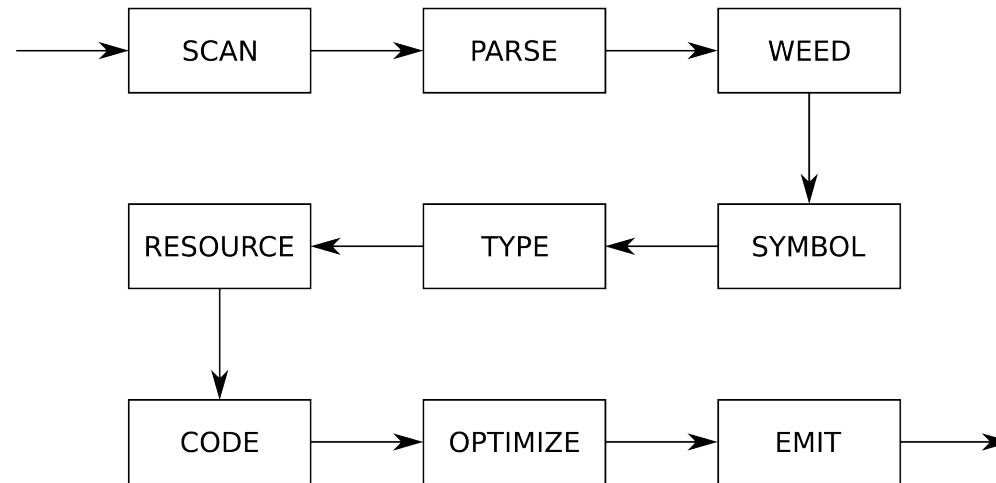
# Background on Programming Languages - Statements

A *statement* is a programming language construct which gives structure to expressions and defines the flow of execution

- Control-flow constructs: if, while, for, ...
- Assignments
- Declarations (maybe)
- Expression statements (e.g. `foo();`)
- ...

# Recap on Phases of the Compiler

A compiler is a **modular** pipeline of phases, with each phase handling different concerns.



The frontend of the compiler consists (informally) of the following phases and their responsibilities:

- **Scanning:** Verifying the source input characters and producing tokens;
- **Parsing:** Verifying the sequence of tokens and associating related tokens;
- **Symbol/Type:** Verifying the type correctness of expressions and their use in statements

**Important:** A grammar specifies the definition of “groupings” of non-terminals and terminals *without* types! Types are *semantic* information, and left to a later phase of the compiler.

(We could do so for some cases, but it will explode the size of the grammar)

# Assignment 1

## Questions

- Who is using `flex+bison`? `SableCC`?
- Any questions about the tools?
- What stage is everyone at: scanner, tokens, parser?
- Any questions about the language?
- Any questions about the requirements?

## Notes

- Use the assignment template (<https://github.com/comp520/Assignment-Template>)
- Make sure it runs using the scripts!
- Include in your README file, *all* resources that were consulted, or state “I worked alone”
- No AST building or typechecking in this assignment

# ASTs

## Internal Representations

Building ASTs

Bison

SableCC (*Optional*)

Pretty Printing





# Compiler Architecture

- A compiler *pass* is a traversal of the program; and
- A compiler *phase* is a group of related passes.

## One-pass compiler

A *one-pass* compiler scans the program only once - it is naturally single-phase. The following all happen at the same time

- Scanning
- Parsing
- Weeding
- Symbol table creation
- Type checking
- Resource allocation
- Code generation
- Optimization
- Emitting

# Compiler Architecture

This is a terrible methodology!

- It ignores natural modularity;
- It gives unnatural scope rules; and
- It limits optimizations.

## Historically

It used to be popular for early compilers since

- It's fast (if your machine is slow); and
- It's space efficient (if you only have 4K).

A modern *multi-pass* compiler uses 5–15 phases, some of which may have many individual passes: you should skim through the optimization section of `'man gcc'` some time!

# Intermediate Representations

A multi-pass compiler needs an *intermediate representation* of the program between passes that may be updated/augmented along the pipeline. It should be

- An accurate representation of the original source program;
- Relatively compact;
- Easy (and quick) to traverse; and
- In optimizing compilers, easy and fruitful to analyze and improve.

## In practice

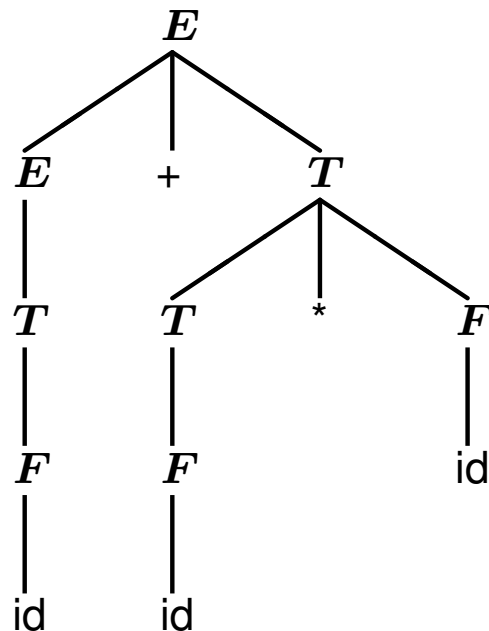
These are competing demands, so some intermediate representations are

- More suited to certain tasks than others; and
- More suited to certain languages than others.

In this class, we focus on tree representations.

## Concrete Syntax Trees

A parse tree, also called a *concrete syntax tree* (CST), is a tree formed by following the exact CFG rules. Below is the corresponding CST for the expression  $a+b*c$

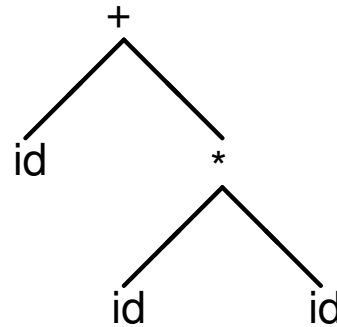


Note that this includes a lot of information that is not necessary to understand the original program

- Terms and factors were introduced for associativity and precedence; and
- Tokens  $+$  and  $*$  correspond to the type of the  $E$  node.

# Abstract Syntax Trees

An *abstract syntax tree* (AST), is a much more convenient tree form that represents a more abstract grammar. The same  $a+b*c$  expression can be represented as



In an AST

- Only important terminals are kept; and
- Intermediate non-terminals used for parsing are removed.

This representation is thus *independent* of the syntax and *independent* of the grammar.

# Constructing an AST

Designing the right AST nodes is important for later phases of the compiler as they will extensively use the AST. The set of AST nodes should

- Represent all distinct programming language constructs; and
- Be minimal, avoiding excess intermediate nodes (e.g. terms and factors).

A concise AST will have ~1 node type for each type of programming language construct.

## Example

In MiniLang the main construct types are declarations, statements, and expressions. The AST would therefore include

- `[Program]`
- `[Declaration]`
- `Statement`
- `Expression`

# Constructing an AST

Language constructs may be several variants (e.g. mathematical expressions  $+$ ,  $-$ ,  $*$ ,  $/$ , unary  $-$ )

## Solutions

1. Inefficient: Create a separate expression node for each kind

- AddExpression;
- MinusExpression;
- TimesExpression;
- DivideExpression;
- UnaryMinusExpression;

**Problem:** Large duplication of near identical code (traversal and AST)

2. Preferred: Create a parametrized expression

- Expression(op);

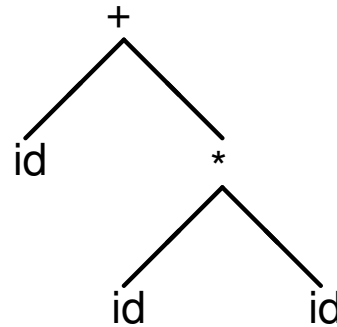
**Slight problem:** There may be special cases which have distinct functionality

**Why not use different nodes for each kind?** Repetitive traversal code and structures

**Why not use a single node for all constructs?** Lack of type information to constrain methods

## Intermediate Language

Alternatively, instead of constructing the tree a compiler can generate code for an internal compiler-specific grammar, also known as an *intermediate language*.



Early multi-pass compilers wrote their IL to disk between passes. For the above tree, the string `+(id, *(id, id))` would be written to a file and read back in for the next pass.

It may also be useful to write an IL out for debugging purposes.



# Examples of Intermediate Languages

- Java bytecode
- C, for certain high-level language compilers
- Jimple, a 3-address representation of Java bytecode specific to Soot, created by Raja Vallee-Rai at McGill
- Simple, the precursor to Jimple, created for McCAT by Prof. Hendren and her students
- Gimple, the IL based on Simple that `gcc` uses
- LLVM-IR

In this course, you will generally use an AST as your IR without the need for an explicit IL.

*Note: somewhat confusingly, both industry and academia use the terms IR and IL interchangeably.*

# ASTs

Internal Representations

**Building ASTs**

Bison

SableCC (*Optional*)

Pretty Printing



## Building IRs

Intuitively, as we recognize parts of the source program during parsing, we assemble them into an IR.

- Requires extending the parser; and
- Executing *semantic actions* during the process.

### Semantic actions

- Arbitrary actions executed during the parser execution.

In other words, each time we recognize part of the source program (i.e. apply a reduction), the semantic action creates a new tree for this portion of the program.

# Building IRs

Each time a semantic action is applied, it produces a *semantic value*.

## Semantic values

Values associated with terminals and non-terminals;

- **Terminals:** provided by the scanner (base case);
- **Non-terminals:** created by the parser;

Each semantic value is thus the root of a subtree in the AST!

Once the entire AST is formed (reduced to the root)

- Tokens form the leaves of the tree; and
- Variables form the internal nodes

**Note:** Not all non-terminals have distinct node types, this is an **AST** after all!

## Building IRs - LR Parsers

When a bottom-up parser executes it maintains a

- *Syntactic stack* – the working stack of symbols; and a
- *Semantic stack* – the values associated with each grammar symbol on the syntactic stack.

We use the semantic stack to recursively build the AST, executing semantic actions on *reduction*.

### In your code

A reduction using rule  $A \rightarrow \gamma$  executes a semantic action that

- Synthesizes symbols in  $\gamma$ ; and
- Produces a new node representing  $A$

In other words, each time we apply a reduction, the semantic action merges subtrees into a new rooted tree. Using this mechanism, we can build an AST.

# ASTs

Internal Representations

Building ASTs

**Bison**

SableCC (*Optional*)

Pretty Printing



## Constructing an AST with flex/bison

Begin defining your AST structure in a header file `tree.h`. Each node type is defined in a `struct`

```
typedef struct EXP EXP;
struct EXP {
    ExpressionKind kind;
    union {
        char *identifier;
        int intLiteral;
        struct { EXP *lhs; EXP *rhs; } binary;
    } val;
};
```

### Node kind

For nodes with more than one kind (i.e. expressions), we define an enumeration `ExpressionKind`

```
typedef enum {
    k_expressionKindIdentifier,
    k_expressionKindIntLiteral,
    k_expressionKindAddition,
    k_expressionKindSubtraction,
    k_expressionKindMultiplication,
    k_expressionKindDivision
} ExpressionKind;
```

### Node value

Node values are stored in a union. Depending on the node kind, a different part of the union is used.

## Constructing an AST with flex/bison

Next, define constructors for each node type in `tree.c`

```
EXP *makeEXP_intLiteral(int intLiteral)
{
    EXP *e = malloc(sizeof(EXP));
    e->kind = k_expressionKindIntLiteral;
    e->val.intLiteral = intLiteral;
    return e;
}
```

The corresponding declaration goes in `tree.h`

```
EXP *makeEXP_intLiteral(int intLiteral);
```



## Constructing an AST with flex/bison

Finally, we can extend `bison` to include the tree-building actions in `tiny.y`.

### Semantic values

For each type of semantic value, add an entry to `bison`'s union directive

```
%union {
    int int_val;
    char *string_val;
    struct EXP *exp;
}
```

For each token type that has an associated value, extend the token directive with the association.

For non-terminals, add `%type` directives

```
%type <exp> program exp
%token <int_val> tINTVAL
%token <string_val> tIDENTIFIER
```

### Semantic actions

```
exp : tINTVAL      { $$ = makeEXP_intLiteral($1); }
    | exp '+' exp  { $$ = makeEXP_plus($1, $3); }
```

# Using an AST

Traversing an AST is done using a set of mutually recursive functions, each switching on the kind and performing the appropriate action.

```
/* pretty.h */
void prettyEXP (EXP *e);

/* pretty.c */
void prettyEXP (EXP *e)
{
    switch (e->kind) {
        case k_expressionKindIdentifier:
            printf("%s", e->val.identifier);
            break;
        case k_expressionKindIntLiteral:
            printf("%i", e->val.intLiteral);
            break;
        case k_expressionKindAddition:
            printf("(");
            prettyEXP (e->val.binary.lhs);
            printf("+");
            prettyEXP (e->val.binary.rhs);
            printf(")");
            break;
        [...]
    }
}
```

# LALR(1) Lists

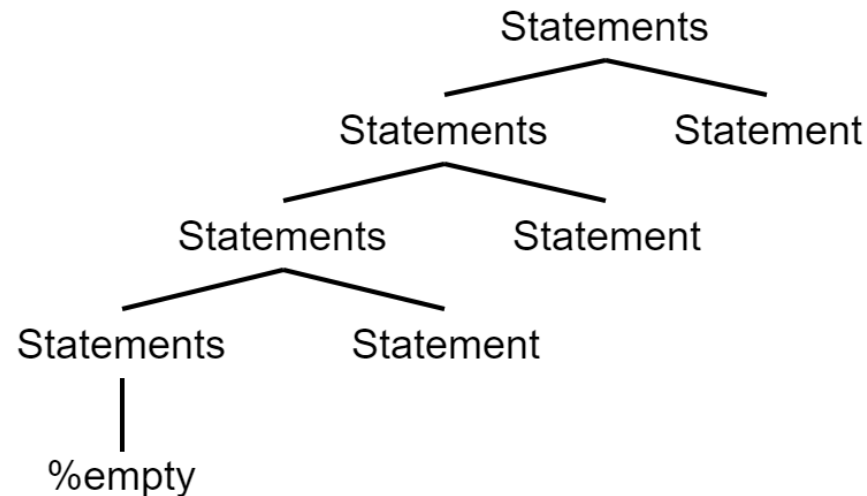
LALR grammars typically build lists using left-recursion, largely for efficiency. Consider the following example for lists of expressions

```

statements : %empty { $$ = NULL; }
           | statements statement { $$ = $2; $$->next = $1; }
;

statement : tIDENT '=' exp ';' { $$ = makeSTATEMENT_assign($1, $3); }
;

```



The lists are naturally backwards!

# LALR(1) Lists

Processing backwards lists requires head recursion to start with the first element

```
struct STATEMENT {
    StatementKind kind;
    union {
        struct { char *identifier; EXP *value; } assignment;
    } val;
    STATEMENT *next;
};

void traverseSTATEMENT(STATEMENT *s) {
    if (s == NULL) {
        return;
    }

    traverseSTATEMENT(s->next);
    /* TODO: ... */
}
```

What effect would a call stack size limit have?

# Extending the AST

As mentioned before, a modern compiler uses 5–15 phases. Each phases of the compiler may contribute additional information to the IR.

- **Scanner**: line numbers;
- **Symbol tables**: meaning of identifiers;
- **Type checking**: types of expressions; and
- **Code generation**: assembler code.

# Extending the AST - Manual Line Numbers

If using manual line number incrementing, adding line numbers to AST nodes is simple.

1. Introduce a global `lineno` variable in the `main.c` file

```
int lineno;
int main(){
    lineno = 1; /* input starts at line 1 */
    yyparse();
    return 0;
}
```

2. increment `lineno` in the scanner

```
%{
    extern int lineno;      /* declared in main.c */
}%

%%
[ \t]+      /* no longer ignore \n */
\n         lineno++;      /* increment for every \n */
```

## Extending the AST - Manual Line Numbers

3. Add a `lineno` field to the AST nodes

```
struct EXP {  
    int lineno;  
    [...]  
};
```

4. Set `lineno` in the node constructors

```
EXP *makeEXP_intLiteral(int intLiteral)  
{  
    EXP *e = malloc(sizeof(EXP));  
    e->lineno = lineno;  
    e->kind = k_expressionKindIntLiteral;  
    e->val.intLiteral = intLiteral;  
    return e;  
}
```

# Extending the AST - Automatic Line Numbers

1. Turn on line numbers in `flex` and add the user action

```
%{  
    #define YY_USER_ACTION yylloc.first_line = yylloc.last_line = yylineno;  
%}  
%option yylineno
```

2. Turn on line numbers in `bison`

```
%locations
```

3. Add a `lineno` field to the AST nodes

```
struct EXP {  
    int lineno;  
    [...]  
};
```



## Extending the AST - Automatic Line Numbers

4. Extend each constructor to take an `int lineno` parameter

```
EXP *makeEXP_intLiteral(int intLiteral, int lineno)
{
    EXP *e = malloc(sizeof(EXP));
    e->lineno = lineno;
    e->kind = k_expressionKindIntLiteral;
    e->val.intLiteral = intLiteral;
    return e;
}
```

5. For each semantic action, call the constructor with the appropriate line number

```
exp : tINTVAL { $$ = makeEXP_intLiteral($1, @1.first_line); }
```

Accessing the token location is done using `@<token position>.<attribute>`

# Extending the AST - Comparison

<https://github.com/comp520/Examples/tree/master/flex%2Bbison/linenumbers>

Given the example program `3 + 4`, we expect the expression node to be located on line 1.

## Manual

```
(3[1]+[2]4[1])
```

## Automatic

```
(3[1]+[1]4[1])
```

## What happened?

Semantic actions are executed when a rule is applied (reduction). An expression grammar can only reduce `3 + 4` if it knows the next token - in this case, the newline.

```
makeEXPintconst  
makeEXPintconst  
lineno++  
makeEXPplus
```

# ASTs

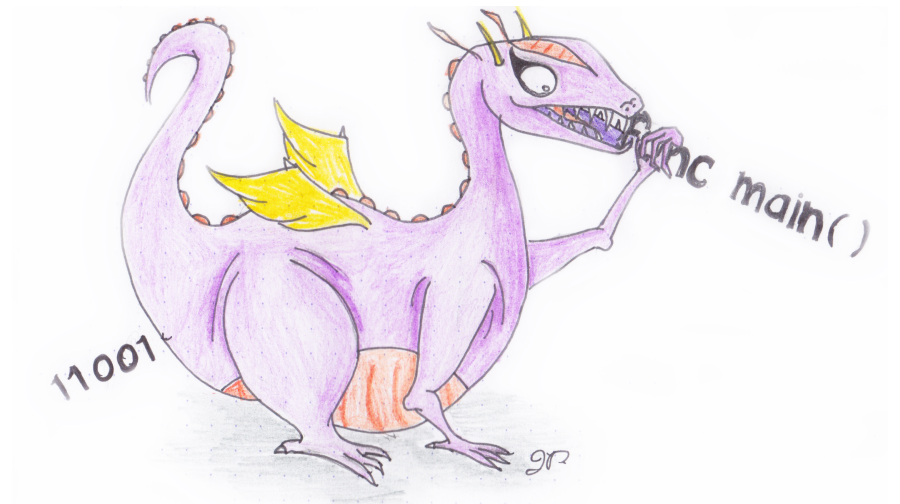
Internal Representations

Building ASTs

Bison

**SableCC (Optional)**

Pretty Printing



# Constructing an AST with SableCC

SableCC 2 automatically generates a CST for your grammar, with nodes for terminals and non-terminals. Consider the grammar for the TinyLang language

## Scanner

```
Package tiny;

Helpers
    tab    = 9;
    cr     = 13;
    lf     = 10;
    digit  = ['0'..'9'];
    lowercase = ['a'..'z'];
    uppercase = ['A'..'Z'];
    letter = lowercase | uppercase;
    idletter = letter | '_' ;
    idchar  = letter | '_' | digit;

Tokens
    eol    = cr | lf | cr lf;
    blank  = ' ' | tab;
    star   = '*';
    slash  = '/';
    plus   = '+';
    minus  = '-';
```

# Constructing an AST with SableCC

```
l_par = '(';  
r_par = ')';  
number = '0' | [digit-'0'] digit*;  
id     = idletter idchar*;
```

Ignored Tokens

```
blank, eol;
```

## Parser

Productions

```
exp    = {plus}    exp plus factor  
       | {minus}   exp minus factor  
       | {factor}  factor;  
  
factor = {mult}    factor star term  
       | {divd}    factor slash term  
       | {term}    term;  
  
term   = {paren}   l_par exp r_par  
       | {id}      id  
       | {number}  number;
```

# Constructing an AST with SableCC

SableCC generates subclasses of 'Node' for terminals, non-terminals and production alternatives

- **Classes for terminals:** 'T' followed by (capitalized) terminal name

`TEol, TBlank, ..., TNumber, TId`

- **Classes for non-terminals:** 'P' followed by (capitalized) non-terminal name

`PExp, PFactor, PTerm`

- **Classes for alternatives:** 'A' followed by (capitalized) alternative name and (capitalized) non-terminal name

`APlusExp (extends PExp), ..., ANumberTerm (extends PTerm)`

Productions

```
exp = {plus}    exp plus factor
     | {minus}  exp minus factor
     | {factor} factor;
```

[...]

# SableCC Directory Structure

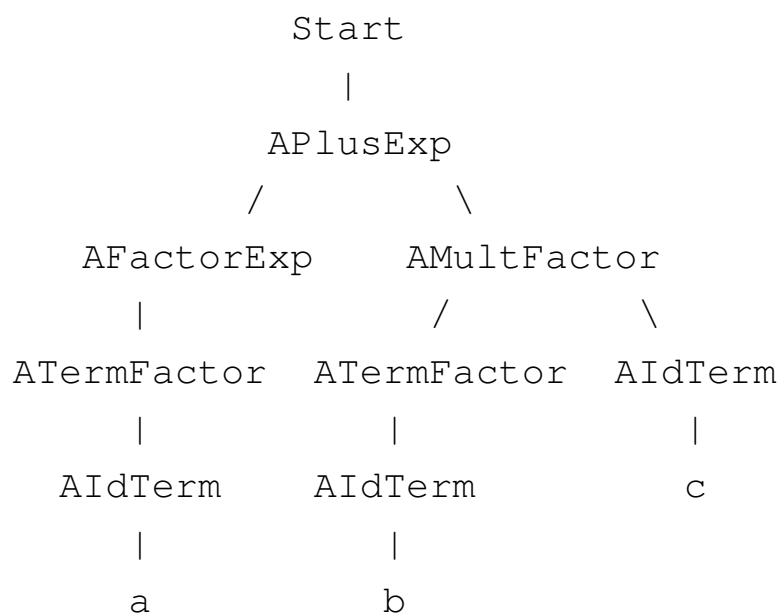
SableCC populates an entire directory structure

```
tiny/
|--analysis/  Analysis.java
|             AnalysisAdapter.java
|             DepthFirstAdapter.java
|             ReversedDepthFirstAdapter.java
|
|--lexer/     Lexer.java lexer.dat
|             LexerException.java
|
|--node/      Node.java TEol.java ... TId.java
|             PExp.java PFactor.java PTerm.java
|             APlusExp.java ...
|             AMultFactor.java ...
|             AParenTerm.java ...
|
|--parser/    parser.dat Parser.java
|             ParserException.java ...
|
|-- custom code directories, e.g. symbol, type, ...
```

## SableCC - Concrete Syntax Trees

Given some grammar, SableCC generates a parser that in turn builds a concrete syntax tree (CST) for an input program.

A parser built from the Tiny grammar creates the following CST for the program 'a+b\*c'

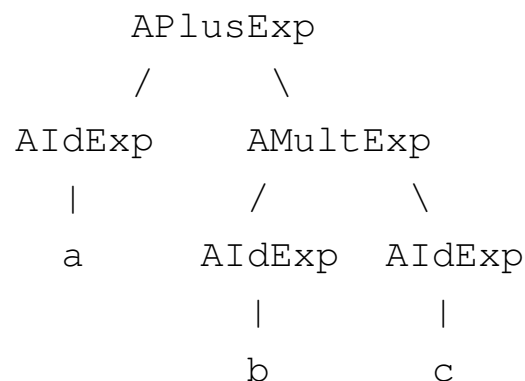


This CST has many unnecessary intermediate nodes. Can you identify them?



## SableCC - Abstract Syntax Trees

We only need an abstract syntax tree (AST) to maintain the same useful information for further analyses and processing



Recall that `bison` relies on user-written actions after grammar rules to construct an AST.

As an alternative, SableCC 3 actually allows the user to define an AST and the `CST→AST` transformations formally, and can then translate CSTs to ASTs automatically.

## Constructing an AST with SableCC

For the TinyLang expression language, the AST definition is as follows

Abstract Syntax Tree

```
exp = {plus}      [l]:exp [r]:exp
     | {minus}    [l]:exp [r]:exp
     | {mult}     [l]:exp [r]:exp
     | {divd}     [l]:exp [r]:exp
     | {id}       id
     | {number}   number;
```

AST rules have the same syntax as productions, except that their elements define the abstract structure. We remove all unnecessary tokens and intermediate non-terminals.

# Constructing an AST with SableCC

Using the AST definition, we augment each production in the grammar with a CST→AST transformations

Productions

```

cst_exp {-> exp} =
    {cst_plus}      cst_exp plus factor
                    {-> New exp.plus(cst_exp.exp, factor.exp) } |
    {cst_minus}     cst_exp minus factor
                    {-> New exp.minus(cst_exp.exp, factor.exp) } |
    {factor}        factor {-> factor.exp};

factor {-> exp} =
    {cst_mult}      factor star term
                    {-> New exp.mult(factor.exp, term.exp) } |
    {cst_divd}      factor slash term
                    {-> New exp.divd(factor.exp, term.exp) } |
    {term}          term {-> term.exp};

term {-> exp} =
    {paren}         l_par cst_exp r_par {-> cst_exp.exp} |
    {cst_id}        id          {-> New exp.id(id) } |
    {cst_number}   number      {-> New exp.number(number) };

```

# Constructing an AST with SableCC

A CST production alternative for a plus node

```
cst_exp = {cst_plus} cst_exp plus factor
```

needs extending to include a CST→AST transformation

```
cst_exp {-> exp} = {cst_plus} cst_exp plus factor  
                  {-> New exp.plus(cst_exp.exp, factor.exp) }
```

- 
- `cst_exp {-> exp}` on the LHS specifies that the CST node `cst_exp` should be transformed to the AST node `exp`.
  - `{-> New exp.plus(cst_exp.exp, factor.exp) }` on the RHS specifies the action for constructing the AST node.
  - `exp.plus` is the kind of `exp` AST node to create. `cst_exp.exp` refers to the transformed AST node `exp` of `cst_exp`, the first term on the RHS.

# Constructing an AST with SableCC

There are 5 types of explicit RHS transformations (actions)

## 1. Getting an existing node

```
{paren} l_par cst_exp r_par {-> cst_exp.exp}
```

## 2. Creating a new AST node

```
{cst_id} id {-> New exp.id(id)}
```

## 3. List creation

```
{block} l_brace stm* r_brace {-> New stm.block([stm])}
```

## 4. Elimination (but more like nullification)

```
{-> Null}
```

```
{-> New exp.id(Null)}
```

## 5. Empty (but more like deletion)

```
{-> }
```

# Constructing an AST with SableCC

Writing down straightforward, non-abstrating CST→AST transformations can be tedious. For example, consider the following production of optional and list elements

```
prod = elm1 elm2* elm3+ elm4?;
```

An equivalent AST construction would be

```
prod{-> prod} = elm1 elm2* elm3+ elm4?  
    {-> New prod.prod(  
        elm1.elm1,  
        [elm2.elm2],  
        [elm3.elm3],  
        elm4.elm4)  
    };
```

## SableCC 3 Documentation

- <http://www.natpryce.com/articles/000531.html>
- <http://sablecc.sourceforge.net/documentation/cst-to-ast.html>

# Announcements (Monday, January 27th)

## Milestones

- Group signup form <https://forms.gle/HgeCthhH3dwD6WmG7>, fill this out over the next week
- How's everyone doing?

## Assignments

- Assignment 1 will be graded soon! Solution programs will be available on myCourses
- Assignment 2 out today! **Due:** Friday, February 7th 11:59 PM

## Midterm

- **Date:** Tuesday, February 25th from 6:00 - 7:30 PM in RPHYS 112
  - Conflicts with: COMP 361D2, COMP 362, MATH 315

# ASTs

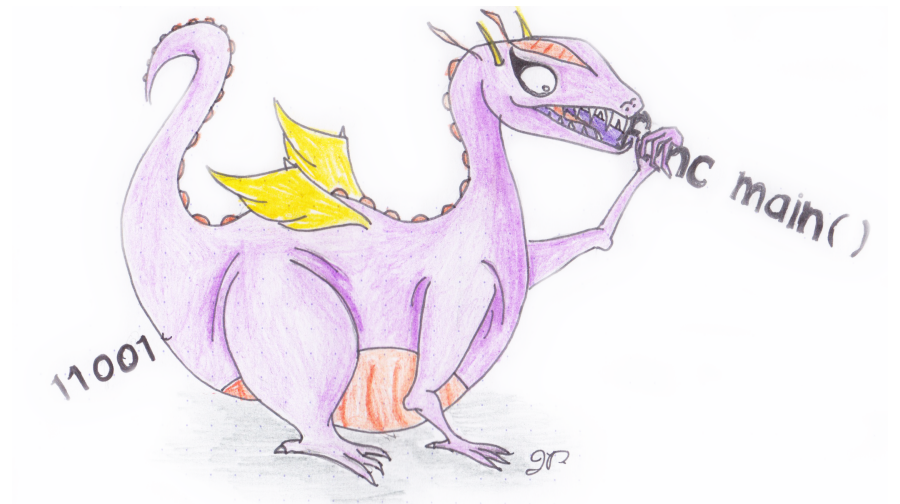
Internal Representations

Building ASTs

Bison

SableCC (*Optional*)

Pretty Printing





# Pretty Printing

Pretty printing is a compiler function that outputs the parsed program in its “original”, “pretty” source form (i.e. in the *original* source language)

The recursive form of ASTs allows us to easily construct recursive traversals as shown below.

```
void prettyEXP (EXP *e)
{
    switch (e->kind) {
        case k_expressionKindIdentifier:
            printf("%s", e->val.identifier);
            break;
        case k_expressionKindIntLiteral:
            printf("%i", e->val.intLiteral);
            break;
        case k_expressionKindAddition:
            printf(" (");
            prettyEXP (e->val.binary.lhs);
            printf("+");
            prettyEXP (e->val.binary.rhs);
            printf(")");
            break;
        [...]
    }
```

# Pretty Printing

Given a parsed AST, invoking the pretty printer starts at the root node.

```
#include "tree.h"
#include "pretty.h"

void yyparse();

EXP *root;

int main()
{
    yyparse();
    prettyEXP(root);
    return 0;
}
```

Pretty printing the expression  $a * (b - 17) + 5 / c$  in TinyLang will output

```
((a * (b - 17)) + (5 / c))
```

**Question:** Why the extra parentheses?

# Pretty Printing

If  $parse(P)$  constructs  $T$  and  $pretty(T)$  reconstructs the text of  $P$ , then

$$pretty(parse(P)) \approx P$$

Even better, we have a stronger relation which says that

$$pretty(parse(pretty(parse(P)))) \equiv pretty(parse(P))$$

Of course, this is a necessary but not sufficient condition for parser correctness.

The testing strategy for a parser that constructs an abstract syntax tree  $T$  from a program  $P$  usually involves a pretty printer, but requires other tests.

## Important observations

- Pretty printers do not output an identical program to the input (whitespace ignored, etc.); and
- Pretty printers should make some effort to be “pretty”.